

The Economics of Solicited and Unsolicited Credit Ratings

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This paper develops a dynamic rational expectations model of the credit rating process, incorporating three critical elements of this industry: (1) the rating agencies' ability to misreport the issuer's credit quality, (2) their ability to issue unsolicited ratings, and (3) their reputational concerns. We analyze the incentives of credit rating agencies to issue unsolicited credit ratings and the effects of this practice on the agencies' rating strategies. We find that issuance of unfavorable unsolicited credit ratings enables rating agencies to extract higher fees from issuers by credibly threatening to punish those that refuse to acquire a rating. Also, issuing unfavorable unsolicited ratings increases the rating agencies' reputation by demonstrating to investors that they resist the temptation to issue inflated ratings. In equilibrium, unsolicited credit ratings are lower than solicited ratings, because all favorable ratings are solicited; however, they do not have a downward bias. We show that, under certain conditions, a credit rating system that incorporates unsolicited ratings leads to more stringent rating standards. (*JEL C73, D82, D83, G24*)

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The role of credit rating agencies as information producers has attracted considerable attention in the last decade. Of particular concern to both investors and regulators is the incentive of credit rating agencies to inflate their ratings to please fee-paying issuers, questioning the effectiveness of reputation as a disciplining device.¹

Among the most controversial aspects of the credit rating industry is the issuance of unsolicited ratings for corporate credit instruments. Unsolicited ratings are published by credit rating agencies “without the request of the issuer or its agent” (Standard & Poor’s 2007). In contrast to solicited ratings, which are requested and paid for by issuers, the issuance of unsolicited ratings does not involve the payment of a rating fee. Unsolicited credit ratings have been widely used since the 1990s and account for a sizeable portion of the total number of credit ratings.²

Despite the prevalence of unsolicited credit ratings, the agencies’ incentives to issue them are not well understood. In a speech given in 2005, then-Chief Economist of the U.S. Securities and Exchange Commission Chester Spatt argued that “from an incentive compatibility perspective, this [practice] would appear to weaken the incentive constraint that encourages a firm to pay for being rated; this suggests that it is puzzling that the rating services evaluate companies that do not pay for ratings” (Spatt 2005).³ Credit rating agencies argue that unsolicited ratings should be seen as a service to “meet the needs of the market for broader ratings coverage” (Standard & Poor’s 2007). Issuers, on the other hand, have expressed concern that these ratings—which are sometimes referred to as “hostile ratings”—are used to punish firms that would otherwise not purchase ratings coverage. For example, Herbert Haas, a former chief financial officer of the German insurance company Hannover Re, recalls a 1998 conversation with a Moody’s official who told him that if Hannover paid

¹ For example, credit rating agencies have been criticized for being slow in recognizing the deteriorating financial conditions of Enron and WorldCom in the early 2000s. More recently, they have been accused of bearing some responsibility for the financial crisis of 2007–2009 by having been too lax in the ratings of some structured financial products (e.g., White 2010). These events have prompted regulatory responses through the Credit Rating Agency Reform Act of 2006 and, more recently, certain sections of the Dodd-Frank Wall Street Reform and Consumer Protection Act of 2010.

² Focusing on international issuers that received a credit rating by Standard and Poor’s during the period from 1998 to 2000, Poon (2003) reports that unsolicited ratings have been assigned to 323 out of 595 issuers (53%). Using a more comprehensive data set of international issuers, Bannier, Behr, and Güttler (2010) find that unsolicited ratings account for between 20% and 30% of all ratings issued between 2000 and 2005. For the U.S. market, Gan (2004) estimates that between 1994 and 1998 about 22% of all new issue ratings were unsolicited ratings. This estimate is based on rating fees paid by the issuers; the exact number is not known, because prior to 2004 rating agencies did not typically disclose whether or not a credit rating was solicited by the issuer. Furthermore, by directly looking at Standard and Poor’s RatingsXpress data for the post-2004 period, we find that unsolicited ratings account for about 10% of the ratings between 2004 and 2011.

³ In addition, Chester Spatt suggested that “the most natural way to resolve the puzzle [...] would be if the unsolicited ratings were not as favorable to the rated company as the paid or solicited ratings” so that “the systematic downward bias in unsolicited ratings [is a way to] ‘punish’ firms that would otherwise not purchase ratings.”

for a rating, it “could have a positive impact” on the grade.⁴ This practice seems to be consistent with empirical evidence that shows that unsolicited ratings are, on average, lower than solicited ratings.⁵

In this paper, we develop a dynamic rational expectations model to address the question of why rating agencies issue unsolicited credit ratings and why these ratings are, on average, lower than solicited ratings. We analyze the implications of this practice for credit rating standards, rating fees, and social welfare. Our model incorporates three critical elements of the credit rating industry: (1) the rating agencies’ ability to misreport the issuer’s credit quality, (2) their ability to issue unsolicited ratings, and (3) their reputational concerns.

We focus on a monopolistic rating agency that interacts with a series of potential issuers that approach the credit market to finance their investment projects.⁶ Markets are characterized by asymmetric information in that the firms’ true credit worthiness is private information to the issuers. The credit rating agency evaluates the issuers’ credit quality, that is, their ability to repay investors. The agency makes these evaluations public by assigning credit ratings to issuers in return for a fee. Issuers agree to pay for these rating services only if they believe that their assigned rating substantially improves the terms at which they can raise capital. This creates an incentive for the rating agency to motivate issuers to pay for ratings by strategically issuing inflated ratings. At the same time, investors cannot directly observe the agency’s rating policy. Rather, they use the agency’s past performance, as measured by the debt-repaying records of previously rated issuers, to assess the credibility of the agency’s ratings. The agency’s credibility in the eyes of investors is summarized by the agency’s “reputation.”

The credit rating agency faces a dynamic trade-off between selling inflated ratings to boost its short-term profit and truthfully revealing the firms’ prospects to improve its long-term reputation. Issuing inflated ratings is costly to the rating agency in the long run, because the practice increases the likelihood that a highly rated issuer will not be able to repay its debt, thereby damaging the rating agency’s reputation. This, in turn, lowers the credibility of the rating agency’s

⁴ See *Washington Post* from November 24, 2004, for an article that reports that within weeks after Hannover refused to pay for Moody’s services, Moody’s issued an unsolicited rating for Hannover, giving it a financial strength rating of “Aa2,” one notch below that given by S&P. Over the course of the following two years, Moody’s lowered Hannover’s debt rating first to “Aa3” and then to “A2.” Meanwhile, Moody’s kept trying to sell Hannover its rating services. In March 2003, after Hannover continued to refuse to pay for Moody’s services, Moody’s downgraded Hannover’s debt by another three notches to junk status, sparking a 10% drop in the insurer’s stock price. The scale of this downgrade came as a surprise to industry analysts, especially because the two rating agencies who received payment from Hannover for their rating services, S&P and A.M. Best, continued to give Hannover high ratings. For a more detailed account of this incident, see Klein (2004); additional anecdotal evidence of this practice can be found in Monroe (1987) and Schultz (1993).

⁵ See, e.g., Gan (2004), Poon and Firth (2005), Van Roy (2006), and Bannier, Behr, and Güttler (2010).

⁶ Although we deliberately ignore the effect of competition and the related issue of “ratings shopping” in our analysis, it is important to note that the credit rating industry is a very concentrated and partially segmented market in which three providers (Standard and Poor’s, Moody’s, and Fitch) have a market share of over 90%.

reports, which makes the ratings less valuable to issuers, and thus reduces the fee that the rating agency can charge for the reports in the future. The rating agency's optimal strategy balances higher short-term fees from issuing more favorable reports against higher long-term fees from an improved reputation for high-quality reports. Thus, in our model reputational concerns act as a disciplining device by curbing the agency's incentive to inflate its ratings. This disciplining effect is, however, limited by the fact that, after a default, investors are not able to perfectly distinguish cases of "bad luck" from cases of "bad ratings" (that is, inflated ratings).

Our analysis shows that the adoption of unsolicited credit ratings increases the rating agency's short-term profit, as well as its long-term profit. This result is driven by two reinforcing effects. The ability to issue unsolicited ratings enables the rating agency to charge higher fees for their solicited ratings. The reason is that the rating agency can use its ability to issue unfavorable unsolicited ratings as a credible "threat" that looms over issuers that refuse to pay for the agency's rating services. This threat increases the value of favorable solicited ratings and, hence, the fee that issuers are willing to pay for them.

The credibility of this threat stems from the fact that, by releasing unfavorable unsolicited ratings, the rating agency can demonstrate to investors that it resists the temptation to issue inflated ratings in exchange for a higher fee, thereby improving its reputation. This second effect, in the form of a reputational benefit, gives the rating agency an incentive to release an unsolicited rating in case an issuer refuses to solicit a rating.⁷ Note that this threat is only latent because, in equilibrium, high-quality issuers prefer to acquire favorable solicited ratings. Thus, in equilibrium, the credit rating agency issues unsolicited ratings along with solicited ratings. Because all favorable ratings are solicited, unsolicited credit ratings are lower than solicited ratings. However, they are not downward biased. Rather, they reflect the lower quality of issuers that do not solicit a rating.

The adoption of unsolicited credit ratings also has important welfare implications. We find that whereas rating agencies always benefit from such a policy—because of the higher fees charged—society may not. In particular, we show that, for some parameter values, allowing rating agencies to issue unsolicited ratings leads to less stringent rating standards, thereby enabling more low-quality firms to finance negative NPV projects. This reduces social welfare and raises the cost of capital for high-quality borrowers. Such an outcome is obtained when the increase in rating fees associated with the adoption of unsolicited ratings is sufficiently large so that it outweighs the additional reputational benefit from truthfully revealing the firm's quality. When this increase in rating fees is small (which happens, for example, when the loss in market value due to an unfavorable unsolicited rating is low),

⁷ This reputational benefit associated with unsolicited ratings may also explain why credit rating agencies issue sovereign debt ratings for which they do not receive any direct compensation.

we obtain the opposite result: the ability to issue unsolicited ratings leads to more stringent rating standards, preventing firms from raising funds for negative NPV investments and, hence, improving social welfare. These results suggest that the question of whether credit rating agencies should be allowed to issue unsolicited ratings and, thus, to earn higher fees has no unambiguous answer.

Our paper contributes to the growing body of literature on the role of credit rating agencies and the phenomenon of rating inflation. [Mathis, McAndrews, and Rochet \(2009\)](#) examine the incentives of a credit rating agency to inflate its ratings in a dynamic model of endogenous reputation acquisition. They show that reputational concerns can generate cycles of confidence in which the rating agency builds up its reputation by truthfully revealing its information only to later take advantage of this reputation by issuing inflated ratings. In [Bolton, Freixas, and Shapiro \(2012\)](#), rating inflation emerges from the presence of a sufficiently large number of naive investors who take ratings at face value. [Opp, Opp, and Harris \(2013\)](#) argue that rating inflation may result from regulatory distortions when credit ratings are used for regulatory purposes, such as bank capital requirements. Finally, [Skreta and Veldcamp \(2009\)](#) and [Sangiorgi and Spatt \(2012\)](#) focus on “ratings shopping” as an explanation for inflated ratings. Both papers assume that rating agencies truthfully disclose their information to investors, but the ability of issuers to shop for favorable ratings introduces an upward bias. In [Skreta and Veldcamp \(2009\)](#), investors do not fully account for this bias, which allows issuers to exploit this winner’s curse fallacy. In contrast, [Sangiorgi and Spatt \(2012\)](#) demonstrate that when investors are rational, shopping-induced rating inflation does not have any adverse consequences. Whereas these papers share some important features with ours, the main contribution of our paper is to explicitly address the effect of unsolicited ratings on the rating policy adopted by credit rating agencies and their impact on rating inflation.

A number of empirical papers have shown that unsolicited ratings are significantly lower than solicited ratings, both in the U.S. market and outside the United States.⁸ These studies explore the reasons for this difference based on two hypotheses. The “self-selection hypothesis” argues that high-quality issuers self-select into the solicited rating group, whereas low-quality issuers self-select into the unsolicited rating group. Under this hypothesis, unsolicited ratings are unbiased, and thus they are not unduly “punitive” to issuing firms. In contrast, the “punishment hypothesis” argues that lower unsolicited ratings are a punishment for issuers that do not pay for rating services and are therefore downward biased. Under this hypothesis, given the same rating level, an issuer whose rating is unsolicited should ex post perform better than one whose rating is solicited.

⁸ A partial list includes [Poon \(2003\)](#), [Gan \(2004\)](#), [Poon and Firth \(2005\)](#), [Van Roy \(2006\)](#), and [Bannier, Behr, and Gütler \(2010\)](#).

The findings of these papers provide conflicting evidence. On the one hand, using S&P bond ratings on the international market, [Poon \(2003\)](#) reports that issuers who chose not to obtain rating services from S&P have weaker financial profiles; this is consistent with the “self-selection hypothesis.” [Gan \(2004\)](#) finds no significant difference between the performance of issuers with solicited and unsolicited ratings. This result leads her to reject the “punishment hypothesis” in favor of the “self-selection hypothesis.” On the other hand, [Bannier, Behr, and Güttler \(2010\)](#) cannot reject the “punishment hypothesis” for their sample.

Our paper suggests an alternative explanation for these findings. We show that although unsolicited ratings are lower, they are not the result of rating deflation. Rather, they reflect the lower quality of issuers, as suggested by the self-selection hypothesis. This does not mean, however, that rating agencies cannot use unfavorable unsolicited ratings as a threat to pressure issuers to pay higher fees for more favorable ratings. We show that the rating agency’s ability to issue unfavorable unsolicited ratings to high-quality firms can act as a credible punishment even though it may not be carried out in equilibrium and, hence, may not be observed by investors. This happens because, in equilibrium, the rating agency optimally sets the fee that the agency charges for favorable solicited ratings at a level at which issuers prefer to purchase ratings rather than risk obtaining unfavorable unsolicited ratings.

The remainder of this paper is organized as follows. Section 1 introduces the model. Section 2 describes the equilibrium of the model and analyzes the optimal rating policy in a solicited-only rating system. Section 3 solves for the equilibrium strategies in a rating system that incorporates unsolicited ratings. Section 4 compares the rating agency’s fees and rating standards under the two rating systems and derives implications for social welfare. Section 5 summarizes our contribution and concludes. All proofs are contained in the Appendix.

1. The Model

We consider an economy endowed with three types of risk-neutral agents: firms (or “issuers”), a credit rating agency (CRA), and investors.⁹ The game has two periods, denoted by $t \in \{1, 2\}$. The riskless rate is normalized to zero.

At the beginning of each period, a firm has access to an investment project with probability β (the game tree is displayed in Figures 1 and 2). The project requires an initial investment of I units of capital. Firms have no capital and

⁹ The organizational structure of the credit rating industry is not critical to our analysis. All we need is a market for credit ratings that is not perfectly competitive and a CRA that has some market power, so that in equilibrium the CRA can extract some of the surplus it generates. The presence of these rents makes reputation valuable, allowing reputation to serve as a disciplining device. This is a plausible scenario because in markets in which reputation matters, a “good” reputation is acquired slowly over time and is necessarily in limited supply, making these markets inherently imperfectly competitive. In contrast, perfectly competitive markets are populated by anonymous players, and reputation building plays no role.

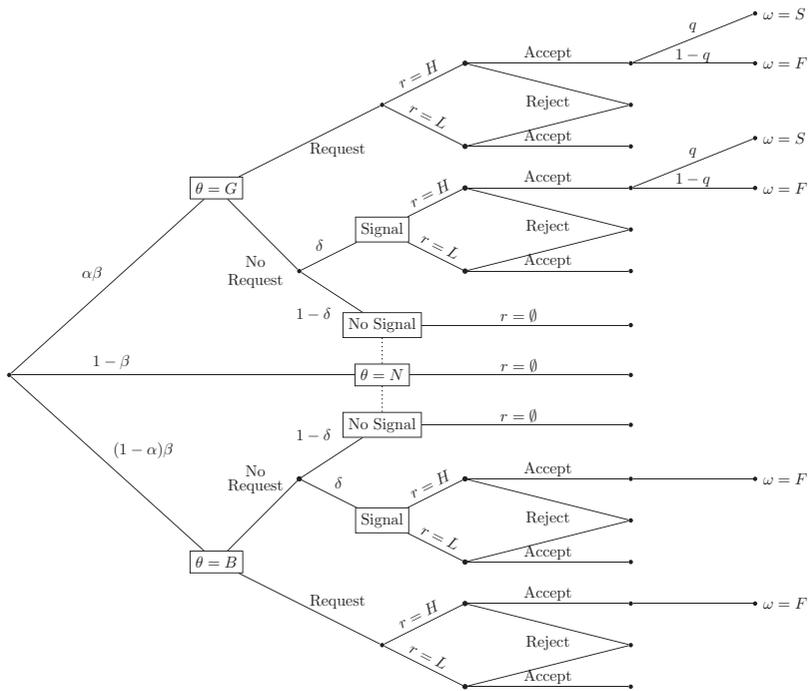


Figure 1
Decision tree in the solicited-only credit rating system

therefore must raise funds from outside investors in perfectly competitive capital markets. If the project is undertaken, it yields an end-of-period payoff of $R > I$ if successful ($\omega = S$) and a payoff of zero if it fails ($\omega = F$), after which the firm is wound down and ceases to exist. The outcome of the project, that is whether the project succeeds or fails, is observable to outside investors. If a firm does not invest, the project vanishes and the firm becomes worthless. Firms that do not have a project in the first period may have a new opportunity to invest in a project in the second period, if they obtain one (which happens again with probability β). Absent a project, the firm has no financing needs and does not access the capital market. Firms maximize the current market value of their shares (net of investment expenses and the rating fee).¹⁰

Investment projects are of heterogeneous quality, where project quality is characterized by its success probability. A type G project (denoted by $\theta = G$) has a success probability of q , whereas a type B project ($\theta = B$) has a success

¹⁰ It is crucial to our analysis that firms care about their short-term market value. Introducing a component based on a firm's long-term profit, however, would not affect our results qualitatively as long as the short-term component is sufficiently important.

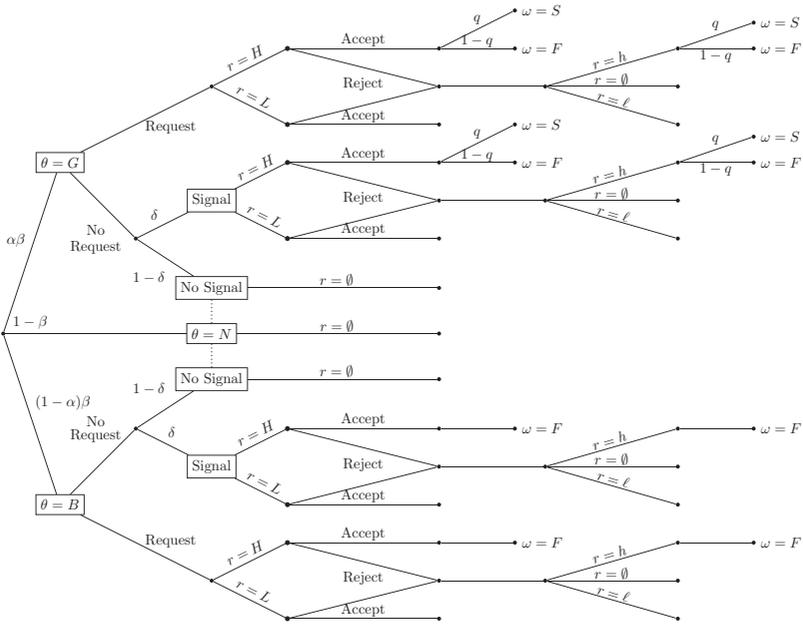


Figure 2
Decision tree in the credit rating system with unsolicited credit ratings

probability of zero.¹¹ Investors believe ex ante that a fraction α of projects are “good” (i.e., of type G) and a fraction $1-\alpha$ are “bad” (i.e., of type B). We assume that, on average, firms have access to positive NPV projects, that is, $\alpha q R - I > 0$. We use $\theta = N$ to denote a firm without a project.

Financial markets are characterized by asymmetric information. Whereas firm insiders know the quality of their own project, outside investors cannot tell a firm with a good project from a firm with a bad one. This creates a role for the CRA: by releasing a “credit rating,” the CRA can reduce the information asymmetry between firms and investors and, possibly, allow firms to raise capital at better terms. We assume that the CRA is able to produce information on a firm’s project that is valuable to investors. This may happen because the CRA has access to private information not available to investors and/or to a superior information production technology that allows the CRA to obtain better estimates of firms’ default and recovery rates. This information production technology may be the outcome, for example, of the CRA’s specialized knowledge in assessing a firm’s credit risk.

¹¹ We focus on the case in which type B projects have zero success probability for expositional simplicity. Extending the analysis to the case in which type B projects succeed with a positive probability of less than q is straightforward, although a bit messier.

We model the credit rating process as follows.¹² At the beginning of each period, a firm that obtained a project decides whether or not to request a credit rating from the CRA. If it requests a rating, the CRA learns the firm's project type at no cost.¹³ If the firm does not request a rating, the CRA observes its project quality only with probability $\delta \in (0, 1)$. With probability $1 - \delta$ the CRA does not observe any signal, and the firm is pooled with firms that do not have an investment project. Thus, the quality of the CRA's information is higher for ratings that were requested by the firm than for those that were not. This assumption captures the notion that, when soliciting a rating, firms make their books available for inspection by the rating agency and hence disclose private information to the agency that is not available to other market participants. In contrast, unsolicited ratings are in many cases just based on public information (and on the CRA's information production technology).¹⁴

Based on its information, the CRA then proposes a credit rating r to the firm. We assume that a credit rating can only be issued for a firm known to have an investment project.¹⁵ This is the case if the firm requested a rating (in which case the CRA learns the firm's project quality) or, in the case the firm did not request a rating, if the CRA has observed an informative signal about the firm (which happens with probability δ). The credit rating can be either "high" ($r = H$) or "low" ($r = L$). The fee ϕ^r charged by the CRA for a rating r is a fraction $\gamma \in (0, 1]$ of the "surplus value" generated by the rating for the firm. This surplus value is the difference between the firm's (net) market value associated with the rating and its market value without such a rating (which will depend on the CRA's equilibrium strategy when the firm refuses to acquire a rating). We assume that γ is the same in both periods and is common knowledge.¹⁶ The prospective rating and the fee are privately proposed by the CRA to the issuing firm and are not observable to investors.

¹² A more detailed description of the rating process can be found in Appendix A.

¹³ Our main results also go through in a setting in which the CRA can observe the signal at positive cost (as long as this cost is not too large). This is driven by the fact that, in equilibrium, the CRA is better off releasing a rating after acquiring information about the rated firm, rather than issuing a rating blindly and thus putting its reputation at risk, as long as the cost of information acquisition is not too high.

¹⁴ We adopt this information structure to model in a parsimonious way the feature that solicited credit ratings are based on better information than unsolicited ones. Our model could be extended by assuming that the signal observed by the CRA about the quality of the firm's project is noisier when the firm does not request a rating.

¹⁵ This can be justified by the fact that, in reality, a credit rating is not just a "notch" on a certain grading scale but is a comprehensive report that describes the firm's business activities, projected cash flows, risk factors, etc., that is, an assessment of the firm's investment opportunity set. This feature also models the observation that firms with a debt rating are only a relatively small group. For example, [Faulkender and Petersen \(2006\)](#) report that on average only 21% of public firms had a debt rating between 1986 and 2000; more recently, [Avramov et al. \(2013\)](#) find that between 1985 and 2008 there were on average 1,931 rated firms out of a universe of approximately 5,000 firms covered by the Center for Research in Security Prices (CRSP).

¹⁶ This compensation rule is adopted to capture, in the simplest way possible, the dependency of the CRA's fee on the incremental value of its ratings. The fraction γ can be thought of as representing the CRA's bargaining power, exogenous to the model, while bargaining with the firm. Alternatively, it may depend on the competitive pressure among CRAs (not modeled here). In a similar vein, [Opp, Opp, and Harris \(2013\)](#) suggest that the outside options of firms are affected by competitive pressure.

The firm can either accept the CRA's offer and pay the fee or decline the offer. If the firm accepts the offer, the CRA collects the rating fee and publicizes the rating as a "solicited credit rating" $r \in \{H, L\}$ to investors. If the firm declines the offer, the firm does not pay the fee. The CRA can then choose to either issue an "unsolicited rating" $r \in \{h, \ell\}$ or to not issue a rating at all (denoted by $r = \emptyset$).¹⁷ Note that if the CRA decides to issue an unsolicited rating, the rating does not have to be the same as the one proposed to the firm.

Credit ratings are important to firms because they affect the terms at which they can raise capital from investors. Investors' valuation of a firm depends on the firm's credit rating, as well as the credibility of the CRA that issued the rating. The latter is important because the CRA cannot commit to truthfully reveal its information about a firm's quality to investors. Rather, it may have an incentive to misreport information that is not directly observable to investors. Investors must therefore decide the extent to which they should trust the CRA and its ratings, based on available information, such as the CRA's past track record.

To capture these ideas in our model, we adopt the "adverse selection" approach to modeling reputations introduced by [Kreps and Wilson \(1982\)](#) and [Milgrom and Roberts \(1982\)](#).¹⁸ In particular, we assume that there are two types of CRAs: ethical ones (denoted by $\tau = e$) and opportunistic ones ($\tau = o$). An ethical CRA is "committed" to truthfully revealing its information about a firm, whether or not a rating is solicited. It always offers to issue an H -rating (h -rating) for firms known to be good and an L -rating (ℓ -rating) for firms known to be bad. An opportunistic CRA, on the other hand, chooses its reporting strategy to maximize its expected profit over the two periods. In all other aspects, the two types of CRAs are identical: they use the same rating categories and charge the same fees.

Investors do not observe the CRA's type and believe that, at the beginning of period 1, the CRA is of the ethical type with probability μ_1 (and is of the opportunistic type with probability $1 - \mu_1$). As investors receive more information about the credit ratings released by the CRA and observe the agency's performance over time, they update their beliefs about the CRA's type (as discussed in the next section).¹⁹

¹⁷ We use lowercase letters for unsolicited ratings to differentiate them from solicited ratings. This reflects the current practice of rating agencies to identify unsolicited ratings as such.

¹⁸ For other applications of this approach in a financial markets setting see, for example, [Diamond \(1989\)](#) and [Chemmanur and Fulghieri \(1994a, 1994b\)](#), among many others.

¹⁹ Although the investors' updating process is driven by the fact that, in each period, there is a single firm that can obtain a credit rating, we want to emphasize that this assumption is not crucial to our results. The presence of multiple rated firms would allow investors to draw sharper inferences about the CRA's type (e.g., [Opp, Opp, and Harris 2013](#)), but would not alter our basic conclusions as long as investors cannot perfectly infer the CRA's type from the observed ratings and default rates.

2. The Solicited-Only Credit Rating System

In this section, we solve for the equilibrium in a rating system with solicited ratings only. In this case, the CRA's rating policy in period t is fully characterized by the vector $\{p_t^G, p_t^B\}$, where p_t^θ denotes the probability that an H -rating is offered to a firm of type $\theta \in \{G, B\}$.

Absent the option of issuing unsolicited ratings, firms that decline to purchase a rating remain unrated. As we will show below, this applies (in equilibrium) to all firms that are offered an L -rating by the CRA. These firms are better off not acquiring a rating, because an L -rating will reveal that they are of the bad type and, hence, that their value is lower than the value of a firm without a project.²⁰ Thus, for expositional simplicity, our discussion below focuses only on the case in which the CRA either issues an H -rating or the firm remains unrated. We let ϕ_t denote the fee that the CRA charges for an H -rating.

We also conjecture (and verify) that in equilibrium all firms with an investment project request a rating, thereby revealing their type to the CRA. Further, the CRA offers a favorable H -rating to all type G firms. Thus, whereas "rating inflation" (that is, type B firms receiving an H -rating) will be part of our equilibrium, "rating deflation" (type G firms receiving an L -rating) will not. We therefore simplify our notation by setting $p_t^G = 1$ and by letting p_t denote the probability that an H -rating is offered to a firm known to be of type B .

We begin our analysis by discussing how the CRA's rating policy affects the agency's reputation. Because an ethical CRA always assigns an H -rating (L -rating) to a type G (type B) firm, whereas an opportunistic CRA may follow a different rating policy, the issuance of a credit rating and the subsequent performance of the rated firm is informative about the CRA's type. Investors update their beliefs about the CRA's type twice in each period: first, after the CRA releases a rating, and second, after investors observe the outcome (i.e., success or failure) of the firm's investment project (if an investment has been made).

Let μ_t denote the CRA's reputation in the eyes of investors at the beginning of period $t \in \{1, 2\}$. The CRA's reputation after it issues an H -rating can be derived from Bayes' rule as follows:

$$\mu_t^H \equiv \text{prob}[\tau = e | r_t = H] = \frac{\mu_t \alpha}{\mu_t \alpha + (1 - \mu_t)(\alpha + (1 - \alpha)\bar{p}_t)}, \quad (1)$$

where \bar{p}_t denotes the investors' beliefs about the CRA's rating strategy p_t . Note that issuing an H -rating lowers the CRA's reputation (i.e., $\mu_t^H < \mu_t$) if $\bar{p}_t > 0$. This loss of reputation reflects the fact that, in equilibrium, an H -rating is more likely to be released by an opportunistic CRA than an ethical one. Correspondingly, after observing an H -rating, investors update the probability

²⁰ Recall that a firm that does not have a project in the first period still has a chance of investing in a type G project in the second period and, thus, has a positive value.

that the firm’s investment project is of the good type to

$$\alpha_i^H \equiv \text{prob} [\theta = G | r_i = H] = \mu_i^H + (1 - \mu_i^H) \frac{\alpha}{\alpha + (1 - \alpha) \tilde{p}_i}. \quad (2)$$

The (gross) market value of an H -rated firm is thus equal to

$$V_i^H = \alpha_i^H q R, \quad (3)$$

which exceeds the amount I invested in the project since $\alpha_i^H \geq \alpha$. It is easy to verify that V_i^H is an increasing function of the CRA’s reputation.

Lack of rating activity by the CRA (i.e., the observation of an unrated firm, $r_i = \emptyset$) is also informative about the CRA’s type.²¹ This is because the absence of a rating can mean either that a firm does not have access to an investment project and, hence, does not have any financing needs, or that the CRA offered to issue an L -rating and the firm declined the offer. From Bayes’ rule, we have

$$\mu_i^\emptyset \equiv \text{prob} [\tau = e | r_i = \emptyset] = \frac{\mu_i(1 - \beta + (1 - \alpha)\beta)}{\mu_i(1 - \beta + (1 - \alpha)\beta) + (1 - \mu_i)(1 - \beta + (1 - \alpha)\beta(1 - \tilde{p}_i))}. \quad (4)$$

Equation (4) shows that, if $\tilde{p}_i > 0$, lack of a rating increases the CRA’s reputation in the eyes of investors (i.e., $\mu_i^\emptyset > \mu_i$). This is because it is a signal to investors that the CRA refrained from issuing a potentially inflated rating, a practice that is more likely to happen when the CRA is ethical.

Absence of rating activity also affects the value of unrated firms. The value of an unrated firm to investors is the weighted average of the value of a firm without an investment project (that never requested a rating) and the value of a firm with a project that was offered an L -rating that was then declined. Because the latter category only consists of type B firms that have zero value, the value of an unrated firm in the first period is equal to

$$V_1^\emptyset = (1 - \beta_1^\emptyset) \bar{V}, \quad (5)$$

where

$$\beta_1^\emptyset \equiv \text{prob} [\theta \neq N | r_i = \emptyset] = \mu_i^\emptyset \frac{(1 - \alpha)\beta}{1 - \beta + (1 - \alpha)\beta} + (1 - \mu_i^\emptyset) \frac{(1 - \alpha)\beta(1 - \tilde{p}_i)}{1 - \beta + (1 - \alpha)\beta(1 - \tilde{p}_i)}. \quad (6)$$

That is, the probability $1 - \beta_1^\emptyset$ represents the investors’ updated belief that an unrated firm is of type $\theta = N$. The variable \bar{V} denotes the value of a firm that does not have an investment project in the first period, which is given by

$$\bar{V} = (\alpha + (1 - \alpha)(1 - \mu_1^\emptyset) \tilde{p}_2) \beta (V_2^H - I - \phi_2), \quad (7)$$

where $V_2^H - I - \phi_2$ is the market value of an H -rated firm in the second period, net of the investment cost, I , and the fee paid to the CRA, ϕ_2 . The

²¹ The absence of a rating, $r = \emptyset$, can be interpreted as a period of time in which the rating activity of the CRA is “lower than usual.”

term $(\alpha + (1 - \alpha)(1 - \mu_1^{\emptyset})\tilde{p}_2)\beta$ reflects the fact that a type G firm receives an H -rating with probability one in the second period, whereas a type B firm receives such a rating only with probability p_2 and only if the CRA turns out to be of the opportunistic type (with probability $1 - \mu_1^{\emptyset}$).

If an investment is made, which in equilibrium happens only if the firm obtains an H -rating, the project payoff is realized at the end of the period and becomes known to investors. After observing the outcome of the investment project, investors update the CRA's reputation once more. Because firms with good projects are successful with probability q , whereas firms with bad projects always fail, the CRA's updated reputation depends on whether or not the investment project succeeds. If the project succeeds, the firm is revealed as being of type G and the CRA's reputation becomes

$$\mu_t^{H,S} \equiv \text{prob} [\tau = e | r_t = H, \omega_t = S] = \frac{\mu_t \alpha q}{\mu_t \alpha q + (1 - \mu_t) \alpha q} = \mu_t. \quad (8)$$

Project success increases the CRA's reputation (i.e., $\mu_t^{H,S} > \mu_t^H$), because opportunistic CRAs may issue H -ratings with positive probability to bad firms that have a lower success probability. In addition, because in our simplified model only good projects succeed and (in equilibrium) all firms with good projects obtain an H -rating, the observation of a successful H -rated project restores the reputation of the CRA to its original level, that is, $\mu_t^{H,S} = \mu_t$. If the project fails, the CRA's updated reputation is

$$\mu_t^{H,F} \equiv \text{prob} [\tau = e | r_t = H, \omega_t = F] = \frac{\mu_t \alpha (1 - q)}{\mu_t \alpha (1 - q) + (1 - \mu_t)(\alpha(1 - q) + (1 - \alpha)\tilde{p}_t)}. \quad (9)$$

Project failure has an adverse effect on the CRA's reputation (i.e., $\mu_t^{H,F} < \mu_t^H$), because an ethical CRA never issues an H -rating for a firm with a bad project. Note that, when updating the CRA's reputation, investors take into account that the failure of an H -rated firm may be the result of "bad luck" (i.e., a good firm failing), rather than of "bad ratings" (i.e., inflated ratings for bad firms). This means that project failure, although negatively affecting the CRA's reputation, does not fully reveal the CRA's type to investors as long as the success probability of good firms, q , is strictly less than one.

We now derive the objective function of the opportunistic CRA. Proceeding backward, in the second (and final) period, the CRA only cares about the profit that it generates from issuing a solicited rating. Thus, the CRA's objective function is

$$\pi_2(\mu_2) = \beta(\alpha + (1 - \alpha)p_2)\phi_2. \quad (10)$$

Note that the second-period profit depends on the CRA's reputation μ_2 through its effect on the fee ϕ_2 that the CRA can charge firms for an H -rating.

In the first period, the opportunistic CRA chooses a rating policy to maximize the sum of the expected profit obtained in periods 1 and 2:

$$\begin{aligned} \pi_1 = & \alpha\beta \left(\phi_1 + q\pi_2(\mu_1^{H,S}) + (1-q)\pi_2(\mu_1^{H,F}) \right) \\ & + (1-\alpha)\beta \left(p_1 \left(\phi_1 + \pi_2(\mu_1^{H,F}) \right) + (1-p_1)\pi_2(\mu_1^\emptyset) \right) + (1-\beta)\pi_2(\mu_1^\emptyset). \end{aligned} \tag{11}$$

The three components reflect the three cases in which the firm has a good project ($\theta = G$), a bad project ($\theta = B$), or no project ($\theta = N$). If the firm has a good project, the CRA always offers to issue an H -rating and thus earns a fee of ϕ_1 in the first period. The expected second-period profit depends on whether or not the project succeeds, because the project outcome affects the CRA's reputation. If the firm has a bad project, the CRA's expected profit depends on whether the CRA offers to issue an H -rating (with probability p_1) or an L -rating (with probability $1 - p_1$). In the former case, the CRA earns a fee of ϕ_1 in the first period and obtains an expected second-period profit that is based on its updated reputation $\mu_1^{H,F}$, because bad projects always fail. In the latter case, the firm declines to acquire the offered L -rating. Thus, the CRA does not earn a rating fee in the first period and enters the second period with a reputation of μ_1^\emptyset . Finally, if the firm has no project, it remains unrated. In this case, the CRA's profit is given by the expected fee it earns in the second period only.

Having characterized the CRA's problem, we can now solve for the perfect Bayesian equilibrium (PBE) of our economy. Formally, a PBE consists of the firm's decision on whether to request a rating, the opportunistic CRA's rating policy, the firm's decision on whether to acquire the offered rating (and, hence, to invest in the project), and a system of beliefs such that (1) the choices made by the firm and the CRA maximize their respective utility, given the equilibrium choices of the other players and the equilibrium beliefs, (2) the beliefs are rational given the equilibrium choices of the agents and are formed using Bayes' rule (whenever possible), and (3) any deviation from the equilibrium strategy by any party is met by beliefs of the other parties that yield a lower expected utility for the deviating party, compared with that obtained in equilibrium.

Proposition 1. In the solicited-only credit rating system, there exists a unique $p_1 \in (0, 1]$ such that the following strategies are an equilibrium:

- (1) All firms with an investment project request a rating. Firms always acquire an H -rating if they are offered one; they never acquire an L -rating rating. Firms raise funds and invest in the project if and only if they obtain an H -rating.
- (2) In period 1, the opportunistic CRA offers an H -rating to type G firms with probability one and to type B firms with probability $p_1 > 0$; it offers an L -rating to type B firms with probability $1 - p_1$. The fee charged for a solicited H -rating is $\phi_1 = \gamma(V_1^H - I - V_1^\emptyset)$. In period 2, the opportunistic

CRA offers an H -rating to all firms that seek financing and charges a fee of $\phi_2 = \gamma(V_2^H - I)$.

These strategies are supported by the off-equilibrium beliefs that firms with an L -rating and firms seeking to raise funds without a rating are of type B with probability one.

Clearly, firms with both good and bad projects prefer to request a rating, because they can always refuse to acquire an L -rating if they are offered one (and pool with type N firms). The credit rating policy of the opportunistic CRA is determined by the following dynamic trade-off. On the one hand, the CRA wants to maximize its current fees by offering an H -rating to all firms with financing needs. The fee for a solicited H -rating is a fraction γ of the “surplus value” created by the CRA, that is, a fraction of the difference between the firm’s market value associated with such a rating, V_t^H , net of the investment cost, I , and its market value without a rating, V_t^\emptyset .²² On the other hand, the CRA wants to preserve, or rather improve, its reputation. Reputation is valuable to the CRA because a better reputation increases the value of securities that are marketed with an H -rating. In this way, a better reputation allows the CRA to charge firms a higher fee for an H -rating in the second period.

The optimal rating policy balances these two effects as follows. In the second period, the opportunistic CRA has no reputational concerns anymore and thus finds that assigning an H -rating to all firms seeking financing is optimal. In the first period, the CRA always issues an H -rating for good firms. Note that although such a policy allows the CRA to pocket the fee ϕ_1 , doing so is potentially costly in terms of the agency’s reputation. Releasing an H -rating immediately reduces the CRA’s reputation from μ_1 to μ_1^H . This loss of reputation is mitigated by the fact that projects of good firms succeed with positive probability and the CRA’s reputation recovers if the project is revealed as successful. However, the agency’s reputation never reaches the level that it could have if the CRA had refused to release an H -rating, μ_1^\emptyset . The fee ϕ_1 charged for a solicited H -rating compensates the CRA for this reputation loss.

The opportunistic CRA also issues H -ratings for some bad firms. The equilibrium value of p_1 trades off the benefits and costs from releasing an H -rating. The benefit of this strategy is that the CRA can pocket the fee ϕ_1 . The cost is the loss of future profits due to a lower reputation, which is now aggravated by the fact that the project of a bad firm fails with probability one. In contrast, if the CRA decides to offer the firm an L -rating, the firm

²² In a credit rating system with solicited ratings only, the outside option of the firm is to remain unrated, generating a value of $V_1^\emptyset > 0$ in the first period and of $V_2^\emptyset = 0$ in the second period. The value of an unrated firm is positive in the first period because the market (correctly) believes that the firm may still obtain a project in the second period. The value of an unrated firm is zero in the second period because the second period is the last period of the game.

will decline the offer and remain unrated, with the effect of increasing the CRA's reputation to μ_1^θ . The opportunistic CRA's incentive to engage in rating inflation ultimately depends on the effectiveness of reputation as a disciplining device, which in turn depends on the loss of reputation caused by the failure of highly rated firms. Because good firms fail with positive probability, this loss of reputation is dampened by the investors' inability to unambiguously attribute a failure to "bad ratings" (i.e., to rating inflation) rather than to just "bad luck."

Proposition 1 shows that the opportunistic CRA offers an H -rating to bad firms with strictly positive probability. The reason is that if it were to mimic the rating strategy of the ethical CRA (and never to issue an H -rating for bad firms), reputation would play no role, because both types of CRAs would adhere to the same rating policy. Thus, the failure of highly rated firms would always be ascribed to "bad luck," rather than to "bad ratings," and would have no effect on the CRA's reputation. Absent the disciplining effect of reputation, the opportunistic CRA would therefore always have an incentive to engage in rating inflation. This argument shows that the imperfect (ex post) observability of a firm's project quality by investors essentially limits the effectiveness of reputation as a disciplining device and that rating inflation is an endemic phenomenon of the credit rating process.

3. The Credit Rating System with Unsolicited Ratings

In a credit rating system that incorporates unsolicited ratings, rating agencies have the ability to issue ratings even if not sponsored by firms. To allow for this possibility, we modify our basic model as follows. If a firm declines the CRA's offer to purchase a rating $r \in \{H, L\}$, the CRA can then decide to publish an unsolicited rating $r \in \{h, \ell\}$ at no cost to the firm.²³ Because, as we will show below, no unsolicited h -ratings (and, again, no solicited L -ratings) are issued in equilibrium, the opportunistic CRA's rating policy in period t can be characterized by the vector $\{\hat{p}_t^\theta, \hat{u}_t^\theta\}$, where \hat{p}_t^θ denotes the probability that the CRA offers an H -rating to a firm of type $\theta \in \{G, B\}$, and \hat{u}_t^θ is the probability that the CRA issues an unsolicited ℓ -rating if the firm refuses to acquire a solicited rating.²⁴ Thus, for ease of exposition, we again focus our discussion on the case in which no firm acquires an L -rating and type G firms request a rating and are offered an H -rating with probability one (i.e., $\hat{p}_t^G = 1$). As in the previous section, we let $\hat{\phi}_t$ denote the fee that the CRA charges for an H -rating and \hat{p}_t the probability that the opportunistic CRA offers such a rating to a type B firm.

²³ Recall that a credit rating can be offered to the firm either if the firm has requested it (in which case the CRA learns the firm's type) or if the firm has not requested it and the CRA has observed an informative signal about the firm's type (which happens with probability δ).

²⁴ We use the "hat" symbol to differentiate the CRA's strategy in the rating system with unsolicited ratings from the CRA's strategy in the solicited-only system.

The possibility of issuing unsolicited credit ratings changes the CRA's strategy space, affecting the investors' updating process about the CRA's reputation and, hence, firm valuations and firm behavior. The key difference with the solicited-only rating system is that firms that are offered an L -rating may no longer be able, by rejecting the offer, to pool with type N firms, if the CRA decides to issue an unsolicited ℓ -rating for them (which, as we will demonstrate below, is indeed part of the CRA's equilibrium strategy). Thus, the ability of the CRA to issue an unsolicited ℓ -rating changes a firm's "outside option."

In a credit rating system with unsolicited ratings, always requesting a credit rating may therefore no longer be optimal for a type B firm. This is because by requesting a rating the firm reveals its type to the CRA, meaning that (in equilibrium) the firm will receive an unsolicited ℓ -rating if it is not offered a solicited H -rating. In contrast, by not requesting a rating, the firm still has the chance to pool with type N firms if the CRA does not observe the firm's type, thereby avoiding an ℓ -rating. Thus, if the probability δ that the CRA observes a signal revealing the firm's type is sufficiently low, not requesting a rating may be optimal for a type B firm. We let $\hat{\lambda}_t$ denote the probability that a type B firm requests a rating in period t .

Issuing an unsolicited rating affects the value of the firm and, at the same time, reveals information about the CRA's type. After observing an unsolicited ℓ -rating, investors update the CRA's reputation as follows:

$$\hat{\mu}_t^\ell \equiv \text{prob} [\tau = e | r_t = \ell] = \frac{\mu_t \Lambda_t^B}{\mu_t \Lambda_t^B + (1 - \mu_t) \Lambda_t^B (1 - \tilde{p}_t) \tilde{u}_t^B}, \quad (12)$$

where $\Lambda_t^B = (1 - \alpha)\beta(\tilde{\lambda}_t + (1 - \tilde{\lambda}_t)\delta)$ denotes the fraction of firms known to be of type B by the CRA—either because they requested a rating (with probability $\tilde{\lambda}_t$) or because the CRA observed an informative signal about their type (with probability $(1 - \tilde{\lambda}_t)\delta$). As before, \tilde{p}_t denotes the investors' beliefs about the opportunistic CRA's equilibrium choice of \hat{p}_t ; \tilde{u}_t^B and $\tilde{\lambda}_t$ now denote their beliefs about \hat{u}_t^B and $\hat{\lambda}_t$, respectively.

Interestingly, the possibility of releasing unsolicited ratings affects the CRA's reputation also when no rating is released (i.e., when $r_t = \emptyset$):

$$\hat{\mu}_t^\emptyset \equiv \text{prob} [\tau = e | r_t = \emptyset] = \frac{\mu_t \Lambda_t^N}{\mu_t \Lambda_t^N + (1 - \mu_t)(\Lambda_t^N + \Lambda_t^B(1 - \tilde{p}_t)(1 - \tilde{u}_t^B))}, \quad (13)$$

where $\Lambda_t^N = 1 - \beta + (1 - \alpha)\beta(1 - \tilde{\lambda}_t)(1 - \delta)$ denotes the fraction of firms believed to not have an investment project by the CRA. It reflects the fact that although an ethical CRA issues a rating for all firms known to have access to an investment project, an opportunistic CRA may choose not to do so.

One can easily verify that the possibility of releasing unsolicited ratings impacts the CRA's reputation after issuing an H -rating only through its effect on (the investors' beliefs about) the probability that a type B firm is offered an

H -rating, which depends on the firm's decision to request a rating. If a bad firm requests a rating, the probability that it is offered an H -rating is \hat{p}_t ; if it does not request a rating, the probability is only $\delta \hat{p}_t$. Thus, the expressions for $\hat{\mu}_t^H$, $\hat{\mu}_t^{H,S}$, and $\hat{\mu}_t^{H,F}$ are identical to those in Equations (1), (8), and (9) when \tilde{p}_t is replaced by $(\tilde{\lambda}_t + (1 - \tilde{\lambda}_t)\delta)\tilde{p}_t$. The same is true for the updated probability $\hat{\alpha}_t^H$ that a firm with an H -rating is of type G in Equation (2).

The objective function of the opportunistic CRA in a credit rating system with unsolicited ratings is similar to the one derived for the solicited-only rating system. In the second period, the CRA's profit again equals the fee that the agency earns by selling an H -rating to a firm.²⁵ In the first period, the objective function now takes into account the possibility that the CRA issues an unsolicited ℓ -rating and that (type B) firms may therefore prefer to not request a rating. Thus, the CRA's expected profit in Equation (11) has to be modified as follows:

$$\begin{aligned} \hat{\pi}_1 = & \alpha\beta \left(\hat{\phi}_1 + q\hat{\pi}_2(\hat{\mu}_1^{H,S}) + (1-q)\hat{\pi}_2(\hat{\mu}_1^{H,F}) \right) \\ & + \Lambda_1^B \left(\hat{p}_1 \left(\hat{\phi}_1 + \hat{\pi}_2(\hat{\mu}_1^{H,F}) \right) + (1-\hat{p}_1) \left(\hat{u}_1^B \hat{\pi}_2(\hat{\mu}_1^\ell) + (1-\hat{u}_1^B)\hat{\pi}_2(\hat{\mu}_1^\theta) \right) \right) \\ & + \Lambda_1^N \hat{\pi}_2(\hat{\mu}_1^\theta). \end{aligned} \tag{14}$$

The possibility of receiving an unsolicited ℓ -rating also affects the firm's decision of whether to request a rating when its project is of type B . By not requesting a rating, a bad firm may be able to conceal its type from the CRA. In particular, it will be mistaken for a type N firm with probability $1 - \delta$, meaning that it will not receive a credit rating in this case. If this happens, its (gross) market value in the first period is equal to

$$\hat{V}_1^\theta = \left(1 - \hat{\beta}_1^\theta\right) \hat{V} = \left(1 - \hat{\beta}_1^\theta\right) \left(\alpha + (1-\alpha)(1 - \hat{\mu}_1^\theta)\tilde{p}_2\right) \beta \left(\hat{V}_2^H(\hat{\mu}_1^\theta) - I - \hat{\phi}_2\right), \tag{15}$$

where $\hat{V}_2^H(\hat{\mu}_1^\theta) = \hat{\alpha}_2^H(\hat{\mu}_1^\theta)qR$ and $\hat{\beta}_1^\theta$ denotes the probability that an unrated firm has an investment project, which is given by

$$\hat{\beta}_1^\theta = \hat{\mu}_1^\theta \frac{(1-\alpha)\beta(1-\tilde{\lambda}_1)(1-\delta)}{\Lambda_1^N} + (1-\mu_1^\theta) \frac{(1-\alpha)\beta(1-\tilde{\lambda}_1)(1-\delta) + \Lambda_1^B(1-\tilde{p}_1)(1-\tilde{u}_1^B)}{\Lambda_1^N + \Lambda_1^B(1-\tilde{p}_1)(1-\tilde{u}_1^B)}. \tag{16}$$

Thus, in the first period, the value of an unrated firm exceeds that of an ℓ -rated firm, which is zero because such firms are known to be bad. On the other hand, if a type B firm requests a rating, it has a chance of receiving an H -rating from an opportunistic CRA (with probability $(1 - \mu_1)\hat{p}_1$), but it may also receive an ℓ -rating (with probability $1 - (1 - \mu_1)\hat{p}_1$). Because $\hat{V}_1^H > \hat{V}_1^\theta > \hat{V}_1^\ell = 0$, the

²⁵ In the second period, all firms with an investment project request a rating (i.e., $\hat{\lambda}_2 = 1$), because the value of their outside option, \hat{V}_2^θ , is zero. This means that the CRA's profit $\hat{\pi}_2$ is again given by Equation (10).

trade-off that a type B firm faces in period 1 is nontrivial. Its optimal decision of whether to request a rating has to be jointly determined with the CRA's equilibrium rating policy.

Type G firms, on the other hand, face the same problem as in the solicited-only rating system: because they receive an H -rating with probability one when their type is known to the CRA, they can only be worse off by not requesting a rating. In the second period, the value of an unrated firm is zero, because the firm has no more chance of realizing a positive NPV project. Thus, all firms with investment projects are better off requesting a rating in the final period. The following proposition characterizes the equilibrium in a credit rating system that allows rating agencies to issue unsolicited ratings.

Proposition 2. In the credit rating system with unsolicited ratings, if $\beta > \alpha/(1-\alpha)$, there exists a pair $(\hat{p}_1, \hat{\lambda}_1) \in [0, 1]^2$ and a threshold $\bar{\mu} > 0$ such that, for any $\mu_1 < \bar{\mu}$, the following strategies are an equilibrium:

- (1) Type G firms always request a rating; type B firms request a rating with probability $\hat{\lambda}_1$ in period 1, and with probability one in period 2. Firms always acquire an H -rating if they are offered one; they never acquire an L -rating. Firms raise funds and invest in the project if and only if they obtain an H -rating.
- (2) In period 1, the opportunistic CRA offers an H -rating to firms known to be of type G with probability one and to firms known to be of type B with probability $\hat{p}_1 \in (0, 1)$; it offers an L -rating to firms known to be of type B with probability $1 - \hat{p}_1$. The fee charged for a solicited H -rating is $\hat{\phi}_1 = \gamma(\hat{V}_1^H - I)$. If a firm rejects the offer to acquire a solicited rating, the CRA issues an unsolicited ℓ -rating for the firm with probability one (i.e., $\hat{u}_1^G = \hat{u}_1^B = 1$). In period 2, the opportunistic CRA offers an H -rating to all firms that seek financing and charges a fee of $\hat{\phi}_2 = \gamma(\hat{V}_2^H - I)$.

These strategies are supported by the off-equilibrium beliefs that firms with an L -rating and firms seeking to raise funds without a rating are of type B with probability one, and that a CRA issuing an unsolicited h -rating is of the ethical type with probability μ_1 (i.e., by the passive conjecture). Further, if $I < \alpha^2 q R$, the pair $(\hat{p}_1, \hat{\lambda}_1)$ is unique.

The ability to issue unsolicited credit ratings affects the firms' and the opportunistic CRA's equilibrium strategies as follows. Firms of type G again prefer to request a rating, knowing that they will be offered an H -rating for sure in this case, rather than to not request a rating and risk being mistaken for a type N firm (which happens with probability $1 - \delta$). In addition, if the CRA is likely to be of the opportunistic type, a type G firm is better off acquiring a solicited H -rating for a fee of $\hat{\phi}_1$, rather than refusing the CRA's offer, hoping to receive an unsolicited h -rating from an ethical CRA for free. For low values of μ_1 , the firm's payoff in the former case, which equals $(1 - \gamma)(\hat{V}_1^H - I)$,

exceeds its expected payoff in the latter case given by $\mu_t(\hat{V}_t^h - I)$, where \hat{V}_t^h is the off-equilibrium market value of a firm with an unsolicited h -rating. In contrast, type B firms play a mixed strategy in period 1 and request a rating with probability $\hat{\lambda}_1$. In an interior equilibrium with $\hat{\lambda}_1 \in (0, 1)$, a type B firm is indifferent between requesting a rating and revealing its type to the CRA, and not requesting a rating and being mistaken for an unrated type N firm with probability $1 - \delta$.

Similar to the case with solicited ratings only, the CRA offers to issue a solicited H -rating for good firms with probability one and for bad firms with strictly positive probability \hat{p}_1 . Firms that decline the offer always receive an unsolicited ℓ -rating (at no cost). Releasing an H -rating again lowers the CRA's reputation, where the loss of reputation is aggravated if the project is a failure and is mitigated if the project turns out to be a success. In contrast, an unsolicited ℓ -rating has a positive effect on the CRA's reputation, even more so than not issuing a rating (or issuing an unsolicited h -rating). This can be seen from Equations (1), (12), and (13), which show that in equilibrium $\hat{\mu}_1^H < \hat{\mu}_1^\theta = \mu_1 < \hat{\mu}_1^\ell$. This result reflects the fact that, in equilibrium, unsolicited ℓ -ratings are more likely to be released by an ethical CRA than by an opportunistic CRA: the former issues unsolicited ℓ -ratings for all firms known to be of type B , whereas the latter does so only for a fraction $1 - \hat{p}_1$ of them. Thus, the issuance of an unsolicited ℓ -rating proves to be a more effective way for the CRA to improve its reputation in the eyes of investors than does the absence of a solicited H -rating: it sends a strong "signal" to investors that the CRA resisted the temptation to issue a possibly inflated H -rating.

It is interesting to note that the beneficial effect of unsolicited ℓ -ratings on the CRA's reputation makes ℓ -ratings a credible threat to firms that refuse to acquire a solicited rating. The threat is credible precisely because these ratings improve the CRA's reputation. This is true for type B firms as well as for type G firms, because neither type of firm can raise the necessary funds to finance its project after receiving an ℓ -rating, which makes any further updating of the CRA's reputation by investors impossible.²⁶ This threat, however, remains "latent" and is not carried out in equilibrium, because all firms are willing to acquire a solicited H -rating (for a fee of $\hat{\phi}_1$) if they are offered one. This means that unsolicited ℓ -ratings are not directly punitive in the sense that they are not issued for good firms, as the following corollary shows.

Corollary 1. In equilibrium, unsolicited ratings are only issued for type B firms. Thus, unsolicited ratings are associated with lower firm valuations,

²⁶ Showing that this argument remains valid in the more general setting in which ℓ -rated firms are still able to obtain financing (and succeed with a (small) positive probability) is straightforward. The reason is that, in equilibrium, investors attribute the success of an ℓ -rated firm to "good luck" rather than to an incorrect rating. This means that the CRA's reputation following the issuance of an ℓ -rating is unaffected by the subsequent observation of a successful project outcome (i.e., $\hat{\mu}_t^\ell = \hat{\mu}_t^{\ell,S}$), making the CRA's threat credible even when firms are still able to invest after obtaining an unfavorable unsolicited rating.

compared with solicited ratings. They are, however, not the result of rating deflation.

Several empirical papers have shown that unsolicited ratings are significantly lower than are solicited ratings (e.g., [Poon 2003](#); [Gan 2004](#); [Poon and Firth 2005](#); [Van Roy 2006](#); [Bannier, Behr, and Güttler 2010](#)).²⁷ However, the reason for this difference is not well understood. Using S&P's bond ratings on the international market, [Poon \(2003\)](#) reports that issuers who chose not to obtain rating services from S&P have weaker financial profiles. Her analysis indicates, however, that the difference in ratings cannot be explained by this self-selection bias, and she concludes that unsolicited ratings are downward biased. [Gan \(2004\)](#) uses an ex post regression approach and finds no significant difference between the performance of issuers with solicited and unsolicited ratings. This result leads her to reject the “punishment hypothesis”—that is, the hypothesis that rating agencies use unfavorable unsolicited ratings to punish firms that refuse to solicit a rating—in favor of the self-selection hypothesis. [Bannier, Behr, and Güttler \(2010\)](#), however, cannot reject the punishment hypothesis for their sample.

Our paper suggests an alternative explanation for these findings. Although unsolicited ratings are lower in our model, they are not the result of rating deflation. Rather, they reflect the lower quality of issuers. As a result, although issuers with unsolicited ratings should have weaker financial profiles, we should not observe any significant differences between their ex post performance and that of issuers with solicited ratings, once we control for their rating level. This argument, however, does not imply that rating agencies do not use unsolicited ratings to threaten issuers to pay higher fees for more favorable ratings. In fact, our analysis shows that, although “punishment” is a latent threat (i.e., it is an out-of-equilibrium outcome) and thus not directly observed by investors, it still plays an important role in the credit rating process as a credible threat. As we will show in Section 4, the presence of such a credible threat allows CRAs to charge higher fees for solicited ratings and, thus, to extract more surplus from firms.

4. Fees, Rating Inflation, and Social Welfare

In this section, we compare the rating fees and rating standards under the two rating systems and discuss their implications for social welfare. We also derive comparative statics results for the opportunistic CRA's rating strategy.²⁸

²⁷ For example, using international data from 1998 to 2000, [Poon \(2003\)](#) shows that although solicited ratings are more common for investment-grade issues (55% of ratings in this category are solicited), unsolicited ratings are the dominant rating type for speculative-grade issues (68% of ratings in this category are unsolicited).

²⁸ As is often the case in games of incomplete information, these results are subject to the caveat that the equilibria characterized in Sections 2 and 3 are not uniquely determined and only exist for certain parameter values.

We begin with a comparison of the rating fees. The following proposition shows that the ability to issue unsolicited ℓ -ratings allows the opportunistic CRA to charge higher fees for solicited H -ratings.

Proposition 3. For a given reputation μ_1 of the CRA, the fee charged for solicited H -ratings is higher in the rating system that allows for unsolicited ratings than in the solicited-only credit rating system, that is, $\hat{\phi}_1 > \phi_1$.

Proposition 3 provides one of the key insights of this paper. The ability to issue unsolicited ratings is valuable to the CRA because it enables the CRA to charge higher fees and, hence, to extract more surplus from rated firms. The reason is that in the solicited-only credit rating system, firms have the option to avoid a low rating by refusing to be rated by the CRA. In this case, the value of the outside option for a firm is the value of an unrated firm, given by Equation (5). If the CRA has the opportunity to issue unsolicited ratings, firms may no longer have this option. By threatening to issue an unsolicited ℓ -rating for all firms that refuse the CRA's offer to acquire a solicited H -rating, the CRA effectively lowers the value of the firm's outside option to the value of a bad firm, which is zero. This increases the value of an H -rating and, hence, the fee that firms pay for the rating.²⁹

We now turn to a comparison of the extent of rating inflation under the two systems. In our model, the extent of rating inflation can be measured by the probability that a type B firm obtains an H -rating from the opportunistic CRA, which is equal to p_1 in the solicited-only rating system and to $(\hat{\lambda}_1 + (1 - \hat{\lambda}_1)\delta)\hat{p}_1$ in the rating system with unsolicited ratings.

Proposition 4. If the fraction of the surplus value captured by the CRA, γ , is sufficiently large, the extent of rating inflation is greater in the solicited-only rating system. For low values of γ , it can be greater in the rating system that incorporates unsolicited ratings.

The rating policy of the opportunistic CRA is determined by a trade-off between a higher current revenue from issuing an H -rating for a type B firm and a better reputation—and hence a higher future revenue—from refusing to do so. Both of these quantities are affected by the possibility of releasing unsolicited ratings. On the one hand, issuing an unsolicited ℓ -rating is a more effective way for the CRA to improve its reputation in the eyes of investors than refraining from issuing a rating. This is because the absence of a rating is partially attributed by investors to the possibility that the firm does not have an investment project. In contrast, issuing an unsolicited ℓ -rating clearly signals to investors that the CRA resisted the temptation to issue an inflated H -rating.

²⁹ Note that this result critically depends on the fact that the issuance of an unsolicited ℓ -rating is a credible threat to firms. As discussed in the previous section, releasing an ℓ -rating is an optimal response for the CRA to a firm's decision not to obtain a solicited rating, independent of the quality of the firm's investment project.

Thus, for a given fee, the possibility of issuing unsolicited ratings strengthens the reputation mechanism. On the other hand, we know from Proposition 3 that the ability to issue unsolicited ratings enables the CRA to charge higher fees for solicited H -ratings, thereby increasing the opportunistic CRA's marginal benefit from issuing an H -rating for a type B firm. When the fraction of the surplus value captured by the CRA is large, the difference in fees that the CRA charges in the two rating systems is small.³⁰ In this case, the positive reputation effect associated with releasing unsolicited ℓ -ratings dominates the difference in fees, making rating inflation less attractive to the CRA. Thus, the extent of rating inflation can be less in a system with unsolicited ratings than in a solicited-only system. This result challenges the notion that higher fees due to the issuance of unsolicited ratings compromise the agencies' rating standards.

Assuming that social welfare is utilitarian (i.e., the social welfare function is equally weighted), social welfare in our model equals the expected NPV of all investment projects undertaken by firms. The following result therefore follows immediately from Proposition 4.

Proposition 5. If the fraction of the surplus value captured by the CRA, γ , is sufficiently large, the adoption of unsolicited credit ratings leads to an improvement in social welfare. For low values of γ , it can lead to a reduction in social welfare.

Proposition 5 sheds some light on the recent debate on whether or not the adoption of unsolicited ratings should be encouraged, and on how such a change would affect social welfare. Our analysis shows that the answer to these questions depends on the fraction of the firms' surplus extracted by the CRA. When the CRA captures a large part of the surplus (i.e., when γ is high), the issuance of unsolicited ratings leads to less rating inflation and, thus, improves social welfare by preventing firms from investing in negative NPV projects.

We conclude this section by deriving comparative statics results for the opportunistic CRA's rating policy, which can be characterized by the probability with which it offers a favorable H -rating to a firm known to be of type B . The following proposition presents results on how p_1 and \hat{p}_1 vary with the model primitives R , q , μ_1 , and γ .

Proposition 6. In both of the credit rating systems, with and without unsolicited ratings, the probability p_1 (respectively, \hat{p}_1) that a firm known by the CRA to be of type B is offered an H -rating increases in the payoff R of successful investment projects, increases in the success probability q of type G projects for low values of q , and decreases in the CRA's reputation μ_1 for

³⁰ This is because a large γ means that the value of an unrated firm in the solicited-only system is close to zero, that is, close to the value of a firm with an unsolicited ℓ -rating.

low values of μ_1 . In addition, it increases in the fraction γ of the surplus value captured by the CRA in the solicited-only rating system and is independent of γ in the rating system with unsolicited ratings.

The opportunistic CRA's rating policy is determined by the first-order condition of the maximization of the CRA's expected profit given by Equation (11) in the solicited-only rating system, and by Equation (14) in the system with unsolicited ratings. In an interior equilibrium, these conditions are given, respectively, by

$$V_1^H - I - V_1^\emptyset = \beta \left(V_2^H(\mu_1^\emptyset) - V_2^H(\mu_1^{H,F}) \right), \quad (17)$$

$$\hat{V}_1^H - I = \beta \left(\hat{V}_2^H(\hat{\mu}_1^\ell) - \hat{V}_2^H(\hat{\mu}_1^{H,F}) \right), \quad (18)$$

where $V_2^H(\mu_2)$ (respectively, $\hat{V}_2^H(\mu_2)$) denotes the value of an H -rated firm in period 2, given that the CRA's reputation equals μ_2 . Inspection of Equations (17) and (18) reveals that the equilibrium rating policy of the opportunistic CRA trades off the immediate benefit of earning a fee of $V_1^H - I - V_1^\emptyset$ (respectively, $\hat{V}_1^H - I$) from issuing an H -rating for a type B firm against a higher future fee due to an improved reputation from not issuing a rating (right-hand side of Equation (17)) or from issuing an unsolicited ℓ -rating (right-hand side of Equation (18)). This trade-off is affected by the model parameters as follows.

An increase in the project payoff R increases the market value of H -rated firms in both periods. In the solicited-only rating system, it also increases the value of a firm's outside option in period 1 of remaining unrated, V_1^\emptyset . The former effect increases the firm's net surplus, whereas the latter effect decreases it. The net effect, however, is positive, which means that an increase in R increases the fee that the CRA can charge for an H -rating under both rating systems.

The positive impact of R on rating fees has two opposing effects on the CRA's optimal strategy. First, the increase in the first-period fee creates an incentive for the opportunistic CRA to issue more H -ratings for bad firms. However, this increase in the first-period fee has to be contrasted with the increase in the second-period fee that the CRA forgoes by issuing an inflated rating. Releasing an H -rating for a type B firm lowers the CRA's reputation in period 2, thereby reducing the agency's expected income from second-period rating fees. Although this reduction in expected second-period fees also increases in the project payoff R , in equilibrium it is dominated by the increase in first-period fees. This makes issuing inflated ratings to bad firms more profitable for the opportunistic CRA.

This property has the interesting implication that, if the project payoff is positively related to the business cycle, rating inflation is procyclical. This means that rating agencies are more likely to issue inflated ratings during

periods of economic expansion, which may lead to lending booms that are associated with lower-quality investments and greater subsequent failures of highly rated securities.³¹

An increase in the success probability q of type G firms has an ambiguous effect on rating inflation. On the one hand, similar to an increase in R , it increases the expected project payoff and, thus, the fee that firms pay for an H -rating. All else equal, this again makes issuing inflated ratings more profitable for the CRA. On the other hand, a higher success probability q means that good projects fail less often, making the detection of rating inflation easier for investors after a project fails: the posterior probability $\mu_1^{H,F}$ is a decreasing function of q . This second effect makes issuing an H -rating for a type B firm more costly for the CRA. When the success probability q is sufficiently small, the first effect dominates the second one, causing p_1 and \hat{p}_1 to be increasing functions of q . For larger values of q , the CRA has to balance the benefits of higher current fees against a more severe reputation loss after a failed project. When the latter exceeds the former, the extent of rating inflation decreases in the success probability q .

In the solicited-only rating system, an increase in the CRA's bargaining power γ always promotes rating inflation. This happens because a higher value of γ allows the CRA to extract a larger fraction of the surplus value from an H -rated firm in period 2, thereby reducing the value of an unrated firm in period 1, V_1^θ . In contrast, in the rating system with unsolicited ratings, the extent of rating inflation does not depend on γ . The reason is that, in this case, firms that refuse to acquire a solicited H -rating receive an unsolicited ℓ -rating, lowering the value of their outside option to zero, the value of a type B firm. Thus, the CRA's rating fees in both periods, given by $\hat{\phi}_t = \gamma(\hat{V}_t^H - I)$, are directly proportional to γ . This implies that γ has no effect on the CRA's optimal choice of rating strategy \hat{p}_1 .

Finally, when the CRA's reputation is sufficiently small (i.e., when μ_1 is close to zero), the informativeness of the CRA's rating record about the agency's type is low. This implies that the CRA's rating strategy has (almost) no effect on its reputation, which weakens the disciplinary role of reputation and leads to less stringent rating standards. Thus, a (small) increase in the CRA's reputation sharpens the investors' inference process and, hence, leads to a reduction in rating inflation.

5. Conclusion

In this paper, we develop a dynamic rational expectations model to address the question of why credit rating agencies issue unsolicited ratings and why these ratings are, on average, lower than solicited ratings. We analyze the

³¹ For a similar result, see Mathis, McAndrews, and Rochet (2009) and Opp, Opp, and Harris (2013).

implications of this practice for credit rating standards, rating fees, and social welfare. Our model incorporates three critical elements of the credit rating industry: (1) the rating agencies' ability to misreport the issuer's credit quality, (2) their ability to issue unsolicited ratings, and (3) their reputational concerns. We focus on a monopolistic rating agency that interacts with a series of potential issuers. In equilibrium, the agency trades off a higher short-term profit from selling inflated ratings to low-quality issuers against a lower long-term profit associated with a reduction in the agency's reputation.

Our analysis shows that the rating agency issues unsolicited ratings for two reasons. First, doing so enables the rating agency to charge higher fees for solicited ratings, because the agency can credibly threaten to punish issuers that refuse to solicit a rating with an unfavorable unsolicited rating. This increases the value of a favorable rating and, hence, the fee that an issuer is willing to pay for it. Second, by issuing a low unsolicited rating, the rating agency can demonstrate to investors that it resists the temptation to issue inflated ratings, thereby improving its reputation.

We demonstrate that, in equilibrium, unsolicited ratings are lower than solicited ratings, because all favorable ratings are solicited. This does not mean, however, that unsolicited ratings have a downward bias. Rather, they reflect the lower quality of firms that do not request a rating.

Comparing credit rating systems with and without unsolicited ratings, we find that although rating agencies benefit from having the option to issue unsolicited ratings, such a system can actually lead to less stringent credit rating standards, thereby reducing social welfare.

Appendix A: Description of the Rating Process

The major rating agencies in the United States—Standard and Poor's, Moody's, and Fitch—all follow a similar rating process. The rating of a corporate issue (or issuer) is typically initiated by the issuer approaching a CRA to rate a particular debt issue (the "request"). The CRA then assembles a team of analysts (the "analytical team") to review pertinent information. This analysis includes the identification of a range of potential factors that could influence the rating of the issue or the issuer as well as a preliminary assessment of these factors (the "pre-evaluation"). The analysts then meet with the issuer's management team to discuss the available information (the "management meeting"). The management meeting is meant to achieve for the CRA a more in-depth understanding of the nature of the firm's business activities and the firm's operating and competitive position, as well as obtain more information about the quality, experience, and risk-taking attitude of the firm's management team. Discussions with the firm's management may continue over time as the rating team needs to obtain additional information. Based on the information collected and the analysis performed by the analytical team, the lead analyst then presents the case to the rating committee and makes a rating recommendation. The rating committee reviews the proposed rating and votes on it (the "committee evaluation"). After voting, the CRA generally provides the issuer with a prepublication rationale for its credit rating (the "notification") that may be appealed by the issuer. Finally, if the issuer agrees to have the rating published, the CRA publishes it as a solicited rating (the "publication"). Note that although solicited credit ratings are clearly sponsored by the issuer (although they may be initiated by the CRA), unsolicited credit ratings

may or may not involve the participation of the issuer in the rating process.³² For further details on the rating process, see Langohr and Langohr (2008), Standard & Poor's (2012), and Moody's (2012).

Appendix B: Proofs

Proof of Proposition 1

A type G firm has no incentive to deviate from its equilibrium strategy by not requesting a rating. Doing so would lower its probability of receiving an H -rating to δ , because it would be mistaken for a type N firm with probability $1 - \delta$ by the CRA. As argued in Section 2, a type B firm also prefers to request a rating: if it requests a rating, it is offered an H -rating with probability p_r ; if it does not request a rating, it is offered an H -rating only with probability δp_r , because it is mistaken for a type N firm with probability $1 - \delta$ by the CRA. Thus, it is optimal to request a rating for both types of firms as long as $V_t^H - I - \phi_t \geq V_t^\theta$, which is the case in equilibrium.

The investors' valuation of an H -rated firm gross of investment expenses, V_t^H , is given by Equation (3), which is based on the updated probabilities μ_t^H and α_t^H . In equilibrium, the investors' beliefs about the CRA's rating policy have to coincide with its actual policy. Thus, $\bar{p}_1 = p_1 > 0$ in Equations (1) and (2). The investors' valuation of an unrated firm in period 1, V_1^θ , is given by Equation (5), where the updated probability β_1^θ in Equation (6) is again based on the equilibrium value $\bar{p}_1 = p_1 > 0$; the value of an unrated firm in period 2, V_2^θ , is zero. Because firms maximize the (net) market value of their shares, the maximum amount that they are willing to pay for an H -rating is therefore given by the difference in valuations, $V_t^H - I - V_t^\theta > 0$, taking into account the investment expenses I of an H -rated firm. By assumption, the CRA's rating fee is a fraction γ of this surplus value, that is, $\phi_t = \gamma (V_t^H - I - V_t^\theta)$, which is independent of the firm's type θ . Further, because firms capture a fraction $1 - \gamma$ of the surplus, they always acquire an H -rating if they are offered one.

Firms never pay for an L -rating. This is supported by the off-equilibrium belief that an L -rated firm is of type B with probability one, which implies that the investors' valuation of such a firm is zero. Thus, firms are better off remaining unrated.

Firms with an H -rating can raise sufficient capital to finance the investment project, because $V_t^H \geq \alpha q R > I$, $t \in \{1, 2\}$. On the other hand, unrated firms are not able to raise the necessary funds, because by doing so, they would reveal to investors that they are of type B and, hence, that their project has a negative NPV.

In period 2, the opportunistic CRA chooses a rating policy p_2^θ , $\theta \in \{G, B\}$, to maximize its expected profit, which is given by

$$\pi_2(\mu_2) = \beta (\alpha p_2^G + (1 - \alpha) p_2^B) \phi_2. \quad (A1)$$

Clearly, because the fee ϕ_2 depends on the investors' beliefs about the CRA's rating policy, rather than its actual policy, this expression is maximized by offering an H -rating to all firms that seek financing (i.e., $p_2^G = p_2^B = 1$).

In period 1, the opportunistic CRA maximizes (a generalized version of) the objective function in Equation (11):

$$\begin{aligned} \pi_1 = & \alpha \beta \left(p_1^G \left(\phi_1 + q \pi_2(\mu_1^{H,S}) + (1 - q) \pi_2(\mu_1^{H,F}) \right) + (1 - p_1^G) \pi_2(\mu_1^\theta) \right) \\ & + (1 - \alpha) \beta \left(p_1^B \left(\phi_1 + \pi_2(\mu_1^{H,F}) \right) + (1 - p_1^B) \pi_2(\mu_1^\theta) \right) \\ & + (1 - \beta) \pi_2(\mu_1^\theta). \end{aligned} \quad (A2)$$

³² For example, Moody's Policy for Designating Unsolicited Credit Ratings in the European Union (effective September 9, 2011) indicates that "solicitation may be evidenced by a request, rating application or contract, payment of fees or confirmation. Participation by the rated entity in the rating process alone does not render a rating solicited" (Moody's 2011).

We prove the optimality of the strategy $p_1^G = 1$ and $p_1^B > 0$ by contradiction. First, suppose that $p_1^B = 0$ (and that $p_1^G > 0$). Then only type G firms receive an H -rating, meaning that the failure of an H -rated firm does not reveal any new information to investors. Thus, $\mu_1^{H,F} = \mu_1^H$. Further, the opportunistic CRA is (weakly) less likely to issue an H -rating than is the ethical CRA, implying that $\mu_1^H \geq \mu_1$ and that $\mu_1^\theta \leq \mu_1$. Thus, the marginal benefit of the opportunistic CRA from issuing an H -rating for a type B firm, which is given by

$$\frac{d\pi_1}{dp_1^B} = (1-\alpha)\beta \left(\phi_1 + \pi_2(\mu_1^{H,F} = \mu_1^H) - \pi_2(\mu_1^\theta) \right), \quad (A3)$$

is strictly positive. This follows from the fact that $\phi_1 > 0$ and that the second-period profit π_2 increases in the CRA's reputation, implying that $\pi_2(\mu_1^{H,F} = \mu_1^H) \geq \pi_2(\mu_1^\theta)$. The strategy $p_1^B = 0$ can therefore not be optimal for the opportunistic CRA.

Next, suppose that $p_1^G < 1$. The fact that $p_1^B > 0$ implies that the opportunistic CRA (weakly) prefers to offer an H -rating to bad firms, that is,

$$\phi_1 + \pi_2(\mu_1^{H,F}) \geq \pi_2(\mu_1^\theta). \quad (A4)$$

However, because the CRA's reputation is higher when an H -rated firm succeeds than when the firm fails (i.e., $\mu_1^{H,S} > \mu_1^{H,F}$), it follows from the above inequality that:

$$\phi_1 + q\pi_2(\mu_1^{H,S}) + (1-q)\pi_2(\mu_1^{H,F}) > \pi_2(\mu_1^\theta). \quad (A5)$$

This shows that the opportunistic CRA strictly prefers to offer an H -rating to a type G firm, contradicting the assumption that $p_1^G < 1$.

Finally, the uniqueness of p_1^B follows from the fact that the marginal benefit of the opportunistic CRA from issuing an H -rating for a type B firm, which has to be equal to zero at an interior solution $p_1^B \in (0, 1)$, is a strictly decreasing function of p_1^B in the interval $[0, 1]$ when $\bar{p}_1 = p_1^B$ (which has to be the case in equilibrium). To see this, note that

$$\frac{d\pi_1}{dp_1^B} = (1-\alpha)\beta \left(\phi_1 + \pi_2(\mu_1^{H,F}) - \pi_2(\mu_1^\theta) \right) \quad (A6)$$

$$= (1-\alpha)\beta\gamma \left((\alpha_1^H + \beta c)qR - I - (1-\beta_1^\theta)\bar{V} \right), \quad (A7)$$

where $\bar{V} = (\alpha + (1-\alpha)(1-\mu_1^\theta))\beta(1-\gamma)(V_2^H - I)$ (see Equation (7)), and the coefficient c is given by

$$c = \frac{\alpha}{1-(1-\alpha)\mu_1^{H,F}} - \frac{\alpha}{1-(1-\alpha)\mu_1^\theta}, \quad (A8)$$

where the probabilities μ_1^θ and $\mu_1^{H,F}$ are defined by Equations (4) and (9), respectively. Equations (2) and (6) show that both α_1^H and β_1^θ are strictly decreasing in p_1^B . From the above definition of c —and the expressions for μ_1^θ and $\mu_1^{H,F}$ in Equations (4) and (9)—we obtain that c is a strictly decreasing function of p_1^B . Further, substituting the expression for V_2^H from Equation (3) into the above expression for \bar{V} , we have

$$\bar{V} = \beta(1-\gamma) \left(\alpha qR - (1-(1-\alpha)\mu_1^\theta)I \right), \quad (A9)$$

which shows that \bar{V} is an increasing function of μ_1^θ and, hence, of p_1^B . This proves that $d\pi_1/dp_1^B$ is a strictly decreasing function of p_1^B . ■

Proof of Proposition 2

The arguments that prove the optimality of the firms' strategies specified in part (1) and the CRA's strategy in part (2) are nearly identical to those given in the proof of Proposition 1 (and are therefore omitted for brevity), with three exceptions: (1) we need to show that type *G* firms prefer to acquire an *H*-rating for a fee of $\hat{\phi}_t$ rather than hoping to receive an unsolicited *h*-rating for free; (2) we have to demonstrate that the opportunistic CRA prefers to issue an unsolicited ℓ -rating if a firm declines the offer to acquire a solicited rating; and (3) we have to take into account that type *B* firms may be better off not requesting a rating (as argued in Section 3). Further, importantly, compared to the solicited-only rating system, the surplus value of a solicited *H*-rating is greater, because firms that refuse to acquire an *H*-rating receive an unsolicited ℓ -rating. Thus, the surplus value is now given by the difference between the value of an *H*-rated firm net of investment expenses, which is $\hat{V}_t^H - I$, and the value of an ℓ -rated firm, which is zero (because, in equilibrium, only type *B* firms with negative NPV projects receive such a rating).

As in the solicited-only rating system, type *B* firms are better off acquiring an *H*-rating if they are offered one; otherwise, they will receive an unsolicited ℓ -rating and thus have zero value. Type *G* firms, on the other hand, may receive an unsolicited *h*-rating after declining the offer to acquire a solicited *H*-rating if the CRA turns out to be of the ethical type (which happens with probability μ_t). In this case, the firm's payoff equals $\hat{V}_t^h - I$, where \hat{V}_t^h is the off-equilibrium market value of a firm with an unsolicited *h*-rating (which depends on the investors' off-equilibrium beliefs but can never exceed qR). Thus, type *G* firms prefer to acquire an *H*-rating if their equilibrium payoff, which is $(1 - \gamma)(\hat{V}_t^H - I)$, exceeds their expected payoff from refusing to do so, which is $\mu_t(\hat{V}_t^h - I)$.³³ Because $\hat{V}_t^H > \alpha qR$ and $\hat{V}_t^h \leq qR$, a sufficient condition for this to be the case is that

$$\hat{\mu}_t \leq (1 - \gamma)(\alpha qR - I)/(qR - I), \quad t \in \{1, 2\}. \tag{A10}$$

Further, because μ_2 is an increasing function of μ_1 and $\mu_2 \leq \hat{\mu}_1^\ell < 1$ for any interior equilibrium $\hat{\rho}_1 \in (0, 1)$ (which we will show below to exist), there exists a $\bar{\mu} > 0$ such that the condition in (A10) holds for any $\mu_1 < \bar{\mu}$. This proves that the strategies specified in Proposition 2 can be sustained as an equilibrium if the probability that the CRA is of the ethical type is sufficiently low.

Next, we show that issuing an unsolicited ℓ -rating is optimal for the opportunistic CRA if a firm declines an offer to acquire a solicited rating. This follows from the fact that the CRA's updated reputation after issuing an unsolicited ℓ -rating, $\hat{\mu}_1^\ell$, strictly exceeds its reputation when no rating is issued, $\hat{\mu}_1^\theta$, or an unsolicited *h*-rating is issued, μ_1 (see Equations (12) and (13)). Note that this is true for type *B* and type *G* firms, because both types of firms cannot raise the necessary capital to invest after receiving an unsolicited ℓ -rating, meaning that no further updating of the CRA's reputation takes place. This proves that the strategies $\hat{u}_1^G = \hat{u}_1^B = 1$ are indeed part of the CRA's equilibrium rating policy.

We now turn to characterizing the equilibrium values of $\hat{\rho}_1$ and $\hat{\lambda}_1$. An interior solution $(\hat{\rho}_1, \hat{\lambda}_1) \in (0, 1)^2$ is characterized by two conditions, (1) the condition that the opportunistic CRA is indifferent between issuing and not issuing a solicited *H*-rating for a type *B* firm, and (2) the condition that a type *B* firm is indifferent between requesting and not requesting a rating. Formally, the pair $(\hat{\rho}_1, \hat{\lambda}_1)$ has to satisfy the conditions $f(\hat{\rho}_1, \hat{\lambda}_1) = 0$ and $g(\hat{\rho}_1, \hat{\lambda}_1) = 0$, where f is the (normalized) marginal benefit of the opportunistic CRA from offering an *H*-rating to a type *B* firm given by

$$f(\hat{\rho}_1, \hat{\lambda}_1) = \frac{1}{\gamma} \left(\hat{\phi}_1 + \hat{\pi}_2(\hat{\mu}_1^{H,F}) - \hat{\pi}_2(\hat{\mu}_1^\ell) \right), \tag{A11}$$

and g is the (normalized) marginal benefit of a type *B* firm from requesting a rating given by

$$g(\hat{\rho}_1, \hat{\lambda}_1) = \frac{1}{1 - \gamma} \left((1 - \mu_1)\hat{\rho}_1 \left(\hat{V}_1^H - I - \hat{\phi}_1 \right) - \hat{V}_1^\theta \right), \tag{A12}$$

³³ Note that μ_t denotes the CRA's reputation in the eyes of a type *G* firm, which in period 2 may differ from the investors' beliefs about the CRA's type. If the firm did not have a project in period 1 (and hence did not receive a rating), the updated reputation from the firm's perspective is μ_1 rather than μ_1^θ .

where $\hat{V}_1^H = \hat{\alpha}_1^H q R$ and \hat{V}_1^θ is defined by Equation (15). The expression for f is similar to the one derived in the proof of Proposition 1, where μ_1^θ is replaced by $\hat{\mu}_1^\ell$. The expression for g follows from the fact that, by requesting a rating, a type B firm gives up its option to remain unrated (and, hence, to have a market value of \hat{V}_1^θ) in favor of potentially receiving an H -rating from an opportunistic CRA (with probability \hat{p}_1), in which case its net market value is $\hat{V}_1^H - I - \hat{\phi}_1$ (in all other cases, it receives an ℓ -rating and has a market value of zero). Of course, this is only relevant if the CRA does not observe a signal that reveals the firm's type. If the CRA observes such a signal, the firm's value is the same whether or not the firm requests a rating.

In addition, there may also exist corner solutions. These solutions can be defined in terms of the functions f and g as follows: $\hat{p}_1 = 1$ is an equilibrium if $f(1, \hat{\lambda}_1) \geq 0$ (recall from the proof of Proposition 1 that $\hat{p}_1 = 0$ cannot be an equilibrium); similarly, $\hat{\lambda}_1 = 0$ is an equilibrium if $g(\hat{p}_1, 0) \leq 0$, and $\hat{\lambda}_1 = 1$ is an equilibrium if $g(\hat{p}_1, 1) \geq 0$.

We proceed by first proving the existence of a pair $(\hat{p}_1, \hat{\lambda}_1)$ that satisfies the above equilibrium conditions and then deriving sufficient conditions for it to be the unique (interior) equilibrium. Substituting the expressions for the firm valuations and rating fees derived in Section 3 into the above expressions for f and g yields

$$f(\hat{p}_1, \hat{\lambda}_1) = \hat{V}_1^H - I + \beta \left(\hat{V}_2^H (\hat{\mu}_1^{H,F}) - I \right) - \beta \left(\hat{V}_2^H (\hat{\mu}_1^\ell) - I \right) \tag{A13}$$

$$= \left(\hat{\alpha}_1^H + \frac{\alpha\beta}{1 - (1-\alpha)\hat{\mu}_1^{H,F}} - \frac{\alpha\beta}{1 - (1-\alpha)\hat{\mu}_1^\ell} \right) qR - I, \tag{A14}$$

$$g(\hat{p}_1, \hat{\lambda}_1) = (1 - \mu_1) \hat{p}_1 \left(\hat{V}_1^H - I \right) - \left(1 - \hat{\beta}_1^\theta \right) \left(1 - (1-\alpha)\hat{\mu}_1^\theta \right) \beta \left(\hat{V}_2^H (\hat{\mu}_1^\theta) - I \right) \tag{A15}$$

$$= (1 - \mu_1) \hat{p}_1 \left(\hat{\alpha}_1^H qR - I \right) - \frac{\beta(1-\beta)}{1 - \beta + (1-\alpha)\beta(1 - \hat{\lambda}_1)(1-\delta)} \left(\alpha qR - (1 - (1-\alpha)\mu_1)I \right), \tag{A16}$$

where we have used the fact that, in equilibrium, $\bar{a}_1^B = 1$, $\hat{\mu}_1^\theta = \mu_1$, and

$$\hat{\alpha}_1^H = \frac{\alpha}{\mu_1\alpha + (1 - \mu_1)(\alpha + (1-\alpha)(\hat{\lambda}_1 + (1 - \hat{\lambda}_1)\delta)\hat{p}_1)}, \tag{A17}$$

$$\hat{\mu}_1^{H,F} = \frac{\mu_1\alpha(1-q)}{\mu_1\alpha(1-q) + (1 - \mu_1)\left(\alpha(1-q) + (1-\alpha)(\hat{\lambda}_1 + (1 - \hat{\lambda}_1)\delta)\hat{p}_1\right)}, \tag{A18}$$

$$\hat{\mu}_1^\ell = \frac{\mu_1}{\mu_1 + (1 - \mu_1)(1 - \hat{p}_1)}. \tag{A19}$$

From Equation (A14), we immediately obtain that, for any $\hat{\lambda}_1 \in [0, 1]$, $f(\hat{p}_1, \hat{\lambda}_1)$ is a continuous and strictly decreasing function of \hat{p}_1 in \mathbb{R}_+ with $f(0, \hat{\lambda}_1) = qR - I > 0$ and $\lim_{\hat{p}_1 \rightarrow \infty} f(\hat{p}_1, \hat{\lambda}_1) = -I < 0$. Thus, for any $\hat{\lambda}_1 \in [0, 1]$, there exists a unique $\hat{p}_1(\hat{\lambda}_1) \in \mathbb{R}_+$ such that $f(\hat{p}_1(\hat{\lambda}_1), \hat{\lambda}_1) = 0$. Let $p_1^*(\hat{\lambda}_1) = \min\{\hat{p}_1(\hat{\lambda}_1), 1\}$ and note that $p_1^*(\hat{\lambda}_1)$ is a continuous and (weakly) decreasing function of $\hat{\lambda}_1$ in the interval $[0, 1]$. This follows from the implicit function theorem because $\frac{\partial f}{\partial \hat{p}_1} < 0$ and $\frac{\partial f}{\partial \hat{\lambda}_1} < 0$ for all $\hat{p}_1, \hat{\lambda}_1 \in [0, 1]$.

Similarly, from Equation (A16), we obtain that, for any $\hat{p}_1 \in [0, 1]$, $g(\hat{p}_1, \hat{\lambda}_1)$ is a continuous and strictly decreasing function of $\hat{\lambda}_1$ in \mathbb{R}_+ . Thus, for any $\hat{p}_1 \in [0, 1]$, there exists at most one $\hat{\lambda}_1(\hat{p}_1) \in [0, 1]$ such that $g(\hat{p}_1, \hat{\lambda}_1(\hat{p}_1)) = 0$. Let $\lambda_1^*(\hat{p}_1) = \hat{\lambda}_1(\hat{p}_1)$ if such a $\hat{\lambda}_1(\hat{p}_1) \in [0, 1]$ exists. If such a $\hat{\lambda}_1(\hat{p}_1)$ does not exist, either $g(\hat{p}_1, 1) > 0$, in which case let $\lambda_1^*(\hat{p}_1) = 1$, or $g(\hat{p}_1, 0) < 0$, in which case let $\lambda_1^*(\hat{p}_1) = 0$.

Using the above definitions of $p_1^*(\hat{\lambda}_1)$ and $\lambda_1^*(\hat{p}_1)$, a strategy pair $(\hat{p}_1, \hat{\lambda}_1)$ is an equilibrium if $\hat{p}_1 = p_1^*(\hat{\lambda}_1)$ and $\hat{\lambda}_1 = \lambda_1^*(\hat{p}_1)$. Note that this definition encompasses interior solutions and corner solutions. To prove the existence of such a fixed point, we show that there exists a $\hat{\lambda}_1 \in [0, 1]$ such that $\lambda_1^*(p_1^*(\hat{\lambda}_1)) = \hat{\lambda}_1$. The existence of such a $\hat{\lambda}_1$ follows from Brouwer's fixed point theorem, because $\lambda_1^*(p_1^*(\hat{\lambda}_1))$ is a continuous function from $[0, 1]$ to $[0, 1]$. This, together with the arguments given in the proof of Proposition 1, prove the existence of a pair $(\hat{p}_1, \hat{\lambda}_1)$ such that the strategies specified in the proposition constitute an equilibrium.

To prove the uniqueness of the strategy pair $(\hat{p}_1, \hat{\lambda}_1)$ if $I \leq \alpha^2 qR$, we show that this condition ensures that $\lambda_1^*(p_1^*(\hat{\lambda}_1))$ is decreasing in $\hat{\lambda}_1$, or equivalently that $\lambda_1^*(\hat{p}_1)$ is increasing in \hat{p}_1 (recall that $p_1^*(\hat{\lambda}_1)$ is decreasing in $\hat{\lambda}_1$). From the implicit function theorem, we obtain that $\hat{\lambda}_1(\hat{p}_1)$, and hence $\lambda_1^*(\hat{p}_1)$, is increasing in \hat{p}_1 if $\frac{\partial g}{\partial \lambda_1} < 0$, which we established above, and $\frac{\partial g}{\partial \hat{p}_1} > 0$. From Equation (A16), we have

$$\frac{\partial g}{\partial \hat{p}_1} = (1 - \mu_1) \left(\left(\hat{\alpha}_1^H + \hat{p}_1 \frac{d\hat{\alpha}_1^H}{d\hat{p}_1} \right) qR - I \right) = (1 - \mu_1) \left((\hat{\alpha}_1^H)^2 qR - I \right). \quad (\text{A20})$$

Because $\hat{\alpha}_1^H \geq \alpha$, the above expression is strictly positive if $I < \alpha^2 qR$.

We conclude the proof by noting that a sufficient condition for the existence of an equilibrium with $\hat{p}_1 < 1$ is that $f(1, 1) < 0$ and $g(1, 1) > 0$, where f and g are defined in Equations (A11) and (A12), respectively. By direct inspection of (A11) and (A12), showing that, for low enough values of μ_1 , we have $g(1, 1) > 0$ as long as the average investment project has a positive NPV (i.e., as long as $\alpha qR > I$, which we assumed at the outset) and $f(1, 1) < 0$ if $\beta > \alpha/(1 - \alpha)$, is straightforward. ■

Proof of Corollary 1

This result follows immediately from Proposition 2. ■

Proof of Proposition 3

We prove this result by first showing that, for $\gamma = 1$, $\hat{\phi}_1$ exceeds ϕ_1 . We then show that the "normalized" fee ϕ_1/γ is increasing in γ for all $\gamma \in (0, 1]$, whereas $\hat{\phi}_1/\gamma$ does not depend on γ . This implies that $\hat{\phi}_1$ exceeds ϕ_1 for all $\gamma \in (0, 1]$.

In the solicited-only credit rating system, the fee charged for an H -rating in the first period is

$$\phi_1 = \gamma \left(V_1^H - I - V_1^\theta \right) = \gamma \left(\alpha_1^H qR - I - (1 - \beta_1^\theta) \bar{V} \right), \quad (\text{A21})$$

whereas in the credit rating system with unsolicited ratings, the fee is

$$\hat{\phi}_1 = \gamma \left(\hat{V}_1^H - I \right) = \gamma \left(\hat{\alpha}_1^H qR - I \right). \quad (\text{A22})$$

If $\gamma = 1$, \bar{V} is equal to zero. Thus, $\hat{\phi}_1 > \phi_1$ if and only if $\hat{\alpha}_1^H > \alpha_1^H$. From the updated probabilities in Equations (1), (2), and (A17), we obtain that this is the case if $(\hat{\lambda}_1 + (1 - \hat{\lambda}_1)\delta)\hat{p}_1 < p_1$. As argued in the proofs of Propositions 1 and 2, in equilibrium the two quantities p_1 and $(\hat{\lambda}_1 + (1 - \hat{\lambda}_1)\delta)\hat{p}_1$ have to satisfy the following constraints (assuming an interior solution):

$$\phi_1 + \pi_2(\mu_1^{H,F}) - \pi_2(\mu_1^\theta) = 0, \quad (\text{A23})$$

$$\hat{\phi}_1 + \hat{\pi}_2(\hat{\mu}_1^{H,F}) - \hat{\pi}_2(\hat{\mu}_1^\ell) = 0. \quad (\text{A24})$$

If $p_1 = (\hat{\lambda}_1 + (1 - \hat{\lambda}_1)\delta)\hat{p}_1$, we immediately obtain that $\phi_1 = \hat{\phi}_1$ and $\pi_2(\mu_1^{H,F}) = \hat{\pi}_2(\hat{\mu}_1^{H,F})$. Further, the expressions for μ_1^θ and $\hat{\mu}_1^\ell$ in Equations (4) and (12) imply that $\mu_1^\theta < \hat{\mu}_1^\ell$ and, thus, that $\pi_2(\mu_1^\theta) < \hat{\pi}_2(\hat{\mu}_1^\ell)$. Hence, for $p_1 = (\hat{\lambda}_1 + (1 - \hat{\lambda}_1)\delta)\hat{p}_1$, the marginal benefit of issuing an H -rating for a type B

firm in the solicited-only case (given by Equation (A23)) exceeds that in the case with unsolicited ratings (given by Equation (A24)). Combined with the fact that the expressions in Equations (A23) and (A24) are decreasing functions of p_1 and $(\hat{\lambda}_1 + (1 - \hat{\lambda}_1)\delta)\hat{p}_1$, respectively (see the proofs of Propositions 1 and 2), this implies that $p_1 > (\hat{\lambda}_1 + (1 - \hat{\lambda}_1)\delta)\hat{p}_1$. Thus, $\hat{\phi}_1 > \phi_1$ when $\gamma = 1$.

The proof of Proposition 2 shows that the equilibrium values of \hat{p}_1 and $\hat{\lambda}_1$, and hence the (normalized) fee $\hat{\phi}_1/\gamma$, do not depend on γ . In contrast, Equation (A21) shows that, for a fixed p_1 , an increase in γ leads to an increase in the (normalized) fee ϕ_1/γ through its effect on \bar{V} (Equation (A9)). Of course, this change in the fee also leads to a change in p_1 . According to the equilibrium condition in (A23), we have

$$\frac{d(\phi_1/\gamma)}{d\gamma} = -\frac{d}{d\gamma} \left(\pi_2(\mu_1^{H,F})/\gamma - \pi_2(\mu_1^\theta)/\gamma \right) = -\frac{\partial}{\partial p_1} \left(\pi_2(\mu_1^{H,F})/\gamma - \pi_2(\mu_1^\theta)/\gamma \right) \frac{dp_1}{d\gamma}, \quad (\text{A25})$$

where the second equality follows from the fact that, for a given p_1 , the (normalized) profit π_2/γ is independent of γ (i.e., π_2/γ depends on γ only through p_1). Because the (normalized) fee ϕ_1/γ is increasing in γ and because the marginal benefit in Equation (A23) is strictly decreasing in p_1 (see the proof of Proposition 1), we obtain from the implicit function theorem that $\frac{dp_1}{d\gamma} > 0$. Further, because $\mu_1^{H,F}$ is decreasing in p_1 and μ_1^θ is increasing in p_1 , we obtain that $\pi_2(\mu_1^{H,F})/\gamma - \pi_2(\mu_1^\theta)/\gamma$ is decreasing in p_1 . This proves that the (normalized) fee ϕ_1/γ is an increasing function of γ , taking into account the indirect effect of γ on the equilibrium value of p_1 . Thus, $\hat{\phi}_1$ exceeds ϕ_1 for all $\gamma \in (0, 1]$. ■

Proof of Proposition 4

In the proof of Proposition 3, we have already shown that $p_1 > (\hat{\lambda}_1 + (1 - \hat{\lambda}_1)\delta)\hat{p}_1$ if $\gamma = 1$. If γ is close to its lower bound of zero (but strictly positive), this result can be reversed. In this case, \bar{V} is large. Thus, for a given level of reputation, the fee that the CRA can charge for an H -rating in the first period is lower in the solicited-only rating system than that being charged in the system with unsolicited ratings (i.e., $\phi_1 < \hat{\phi}_1$) when $p_1 = (\hat{\lambda}_1 + (1 - \hat{\lambda}_1)\delta)\hat{p}_1$. This is true even for values of α close to one:

$$\lim_{\alpha \rightarrow 1} \hat{\phi}_1 - \phi_1 = \lim_{\alpha \rightarrow 1} \gamma(1 - \beta_1^\theta)\bar{V} = \gamma(1 - \gamma)\beta(qR - I) > 0. \quad (\text{A26})$$

In contrast, the difference between the second-period profits in the two cases converges to zero as α goes to one, because $\pi_2(\mu_1^{H,F}) = \hat{\pi}_2(\hat{\mu}_1^{H,F})$ when $p_1 = (\hat{\lambda}_1 + (1 - \hat{\lambda}_1)\delta)\hat{p}_1$ and

$$\lim_{\alpha \rightarrow 1} \hat{\pi}_2(\hat{\mu}_1^\ell) - \pi_2(\mu_1^\theta) = \lim_{\alpha \rightarrow 1} \beta\gamma \left(\frac{\alpha}{1 - (1 - \alpha)\hat{\mu}_1^\ell} - \frac{\alpha}{1 - (1 - \alpha)\mu_1^\theta} \right) qR = 0. \quad (\text{A27})$$

This result follows immediately from Equations (2) and (3). Thus, if α is sufficiently large, the marginal benefit from offering an H -rating to a type B firm in the case with unsolicited ratings, $d\hat{\pi}_1/d\hat{p}_1$, exceeds the marginal benefit in the solicited-only case, $d\pi_1/dp_1$, for all $p_1 = (\hat{\lambda}_1 + (1 - \hat{\lambda}_1)\delta)\hat{p}_1$. From the fact that $d\pi_1/dp_1$ and $d\hat{\pi}_1/d\hat{p}_1$ are decreasing functions of p_1 and $(\hat{\lambda}_1 + (1 - \hat{\lambda}_1)\delta)\hat{p}_1$, respectively (see the proofs of Propositions 1 and 2), we obtain that $p_1 < (\hat{\lambda}_1 + (1 - \hat{\lambda}_1)\delta)\hat{p}_1$. This proves that there exist parameter values such that the extent of rating inflation is greater in the credit rating system with unsolicited ratings. ■

Proof of Proposition 5

If the social welfare function is equally weighted, social welfare is lower the more type B firms obtain an H -rating and invest in their negative NPV projects. Thus, social welfare is directly related to the extent of rating inflation in our model. The result in Proposition 5 therefore follows immediately from Proposition 4. ■

Proof of Proposition 6

In the solicited-only rating system, an interior solution $p_1 \in (0, 1)$ is characterized by the fact that $d\pi_1/dp_1 = 0$ at $p_1 = \hat{p}_1$. Substituting the expression for \bar{V} in Equation (A9) into the expression for $d\pi_1/dp_1$ in Equation (A7), we can rewrite this equality as

$$\left(\alpha_1^H - (1 - \beta_1^\theta)\beta(1 - \gamma)\alpha + \beta c\right)qR - \left(1 - (1 - \beta_1^\theta)\beta(1 - \gamma)(1 - (1 - \alpha)\mu_1^\theta)\right)I = 0, \quad (\text{A28})$$

where the coefficient c is defined in Equation (A8). Because the coefficient of I is clearly negative, this equality can only hold if the coefficient of R is strictly positive. This proves that the marginal benefit $d\pi_1/dp_1$ is an increasing function of the payoff R . From the derivative of the above equation with respect to the success probability q , which is given by

$$\left(\alpha_1^H - (1 - \beta_1^\theta)\beta(1 - \gamma)\alpha + \beta c\right)R + \beta qR \frac{dc}{dq}, \quad (\text{A29})$$

we obtain that $d\pi_1/dp_1$ is also increasing in q , at least for low values of q . (Because $\mu_1^{H,F}$ and hence c are decreasing in q , this result may not hold for large values of q .) Further, from the proof of Proposition 1, we know that $d\pi_1/dp_1$ is a decreasing function of p_1 . Thus, we obtain from the implicit function theorem that the equilibrium probability with which the CRA offers an H -rating to a type B firm is increasing in R and increasing in q for low values of q .³⁴

Because $V_2^H > I$, we obtain from Equation (A7) that the marginal benefit $d\pi_1/dp_1$ is increasing in γ , the fraction of the surplus value captured by the CRA. This, together with the fact that $d\pi_1/dp_1$ is decreasing in p_1 , implies that the equilibrium probability p_1 is increasing in γ as well.

The comparative statics result with respect to the CRA's reputation μ_1 follows from the fact that, for $\mu_1 = 0$, no updating of the CRA's reputation takes place. Thus, $\mu_1^{H,F} = \mu_1^\theta$ and, consequently, $\pi_2(\mu_1^{H,F}) = \pi_2(\mu_1^\theta)$, implying that the CRA's marginal benefit in Equation (A7) is proportional to the fee ϕ_1 , which is strictly positive for all $\hat{p}_1 \in [0, 1]$. This proves that the equilibrium value of p_1 converges to one as μ_1 goes to zero and, thus, that p_1 is a decreasing function of μ_1 for values of μ_1 close to zero.

From the proof of Proposition 2, we know that an interior solution $(\hat{p}_1, \hat{\lambda}_1) \in (0, 1)^2$ in the rating system with unsolicited ratings has to satisfy the conditions $f(\hat{p}_1, \hat{\lambda}_1) = 0$ and $g(\hat{p}_1, \hat{\lambda}_1) = 0$, where f and g are defined in Equations (A11) and (A12), respectively. Applying the implicit function theorem (and Cramer's rule) to this system of equations lets us compute the derivative of \hat{p}_1 with respect to R as

$$\frac{d\hat{p}_1}{dR} = - \frac{\begin{vmatrix} \frac{\partial f}{\partial R} & \frac{\partial f}{\partial \hat{\lambda}_1} \\ \frac{\partial g}{\partial R} & \frac{\partial g}{\partial \hat{\lambda}_1} \end{vmatrix}}{\begin{vmatrix} \frac{\partial f}{\partial \hat{p}_1} & \frac{\partial f}{\partial \hat{\lambda}_1} \\ \frac{\partial g}{\partial \hat{p}_1} & \frac{\partial g}{\partial \hat{\lambda}_1} \end{vmatrix}}. \quad (\text{A30})$$

In the proof of Proposition 2, we have already shown that $\frac{\partial f}{\partial \hat{\lambda}_1} < 0$, $\frac{\partial f}{\partial \hat{p}_1} < 0$, and $\frac{\partial g}{\partial \hat{\lambda}_1} < 0$. If $I < \alpha^2 qR$, we also have that $\frac{\partial g}{\partial \hat{p}_1} > 0$. Thus, to prove that $\frac{d\hat{p}_1}{dR} > 0$, it suffices to show that $\frac{\partial f}{\partial R} > 0$ and $\frac{\partial g}{\partial R} < 0$.

The result that $\frac{\partial f}{\partial R} > 0$ follows immediately from Equation (A14): because the coefficient of I is negative, the equilibrium condition $f(\hat{p}_1, \hat{\lambda}_1) = 0$ can only hold if the coefficient of R is strictly positive.

³⁴ Note that this is trivially true in a weak sense for the corner solution $p_1 = 1$.

To see that $\frac{\partial g}{\partial R} < 0$, note that Equation (A15) can be written as

$$g(\hat{p}_1, \hat{\lambda}_1) = (1 - \mu_1)\hat{p}_1(\hat{\alpha}_1^H q R - I) - \left(1 - \hat{\beta}_1^\theta\right) \left(1 - (1 - \alpha)\hat{\mu}_1^\theta\right) \beta \left(\hat{\alpha}_2^H(\hat{\mu}_1^\theta) q R - I\right). \quad (\text{A31})$$

Because in equilibrium $\hat{u}_1^B = 1$, we have $\hat{\mu}_1^\theta = \mu_1$. This, together with the fact that $(\hat{\lambda}_1 + (1 - \hat{\lambda}_1)\delta)\hat{p}_1 < 1 = (\hat{\lambda}_2 + (1 - \hat{\lambda}_2)\delta)\hat{p}_2$, implies that $\hat{\alpha}_1^H > \hat{\alpha}_2^H(\hat{\mu}_1^\theta)$. Thus, the equilibrium condition $g(\hat{p}_1, \hat{\lambda}_1) = 0$ can only hold if $(1 - \mu_1)\hat{p}_1 < \left(1 - \hat{\beta}_1^\theta\right) \left(1 - (1 - \alpha)\hat{\mu}_1^\theta\right) \beta$. This, however, means that the coefficient of I in Equation (A31) is positive. Hence, the coefficient of R must be negative for an interior equilibrium to exist, proving that $\frac{\partial g}{\partial R} < 0$.

Because the coefficient of R in Equation (A31) is proportional to q , the above argument shows that $\frac{\partial g}{\partial q} < 0$ as well. Further, because the coefficient of R in Equation (A14) can be written as $d(q)q > 0$, we obtain that, for low values of q , $\frac{\partial f}{\partial q} > 0$. (Because $\mu_1^{H,F}$ and hence $d(q)$ are decreasing in q , this result may not hold for large values of q .) Thus, the arguments made above show that $\frac{d\hat{p}_1}{dq} > 0$ as well, at least for low values of q .

The result that the equilibrium probability \hat{p}_1 is independent of γ follows immediately from the fact that neither f nor g is a function of γ .

Finally, analogous arguments to those made above for the solicited-only rating system (where μ_1^θ has to be replaced by $\hat{\mu}_1^\ell$) show that \hat{p}_1 decreases in μ_1 for values of μ_1 close to zero. ■

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